

**EUCLIDEAN GEOMETRY: GRADE 12**

**EUCLIDEAN GEOMETRY QUESTIONS FROM PREVIOUS YEARS' QUESTION PAPERS**

**NOVEMBER 2008**

**QUESTION 7**

7.1 Complete the statements below by filling in the missing word(s) so that the statements are CORRECT:

7.1.1 The angle subtended by a chord at the centre of a circle is . . . . (1)

7.1.2 The angle between the tangent and a chord is . . . . (1)

7.1.3 The opposite angles of a cyclic quadrilateral are . . . . (1)

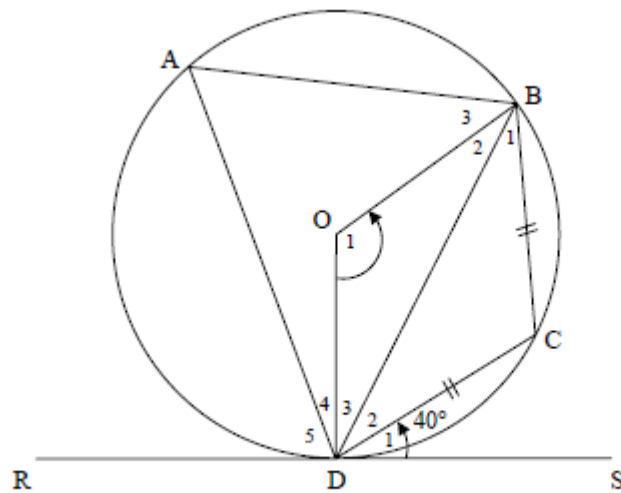
7.2 In the figure below, RDS is a tangent to circle O at D. If  $BC = DC$  and  $\hat{CDS} = 40^\circ$ , calculate, with reasons, the measures of:

7.2.1  $\hat{BDC}$  (2)

7.2.2  $\hat{C}$  (1)

7.2.3  $\hat{A}$  (1)

7.2.4  $\hat{O}_1$  (2)

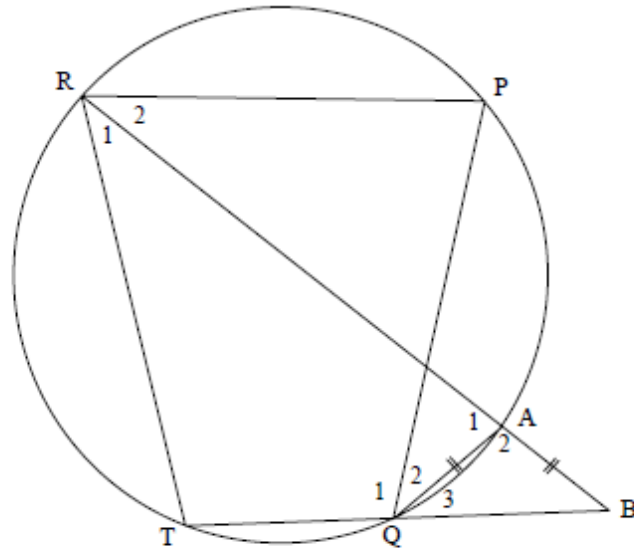


[9]

## EUCLIDEAN GEOMETRY: GRADE 12

### QUESTION 8

In the diagram below, points R, P, A, Q and T lie on a circle. RA bisects  $\hat{R}$  and  $AB = AQ$ . RA and TQ produced meet at B.



Prove that:

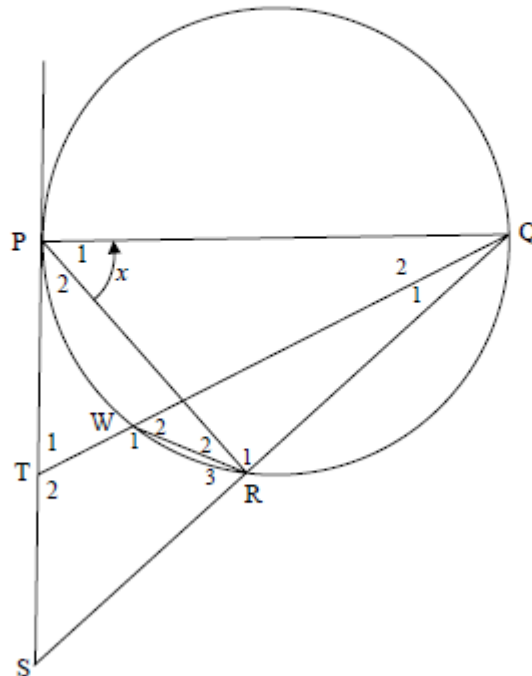
- |            |                        |     |
|------------|------------------------|-----|
| 8.1        | AQ bisects $\hat{PQB}$ | (3) |
| 8.2        | TR = TB                | (2) |
| 8.3        | $\hat{P} = \hat{TRP}$  | (3) |
| <b>[8]</b> |                        |     |

## EUCLIDEAN GEOMETRY: GRADE 12

### QUESTION 9

In the figure below, PQ is a diameter to circle PWRQ. SP is a tangent to the circle at P.

Let  $\hat{P}_1 = x$

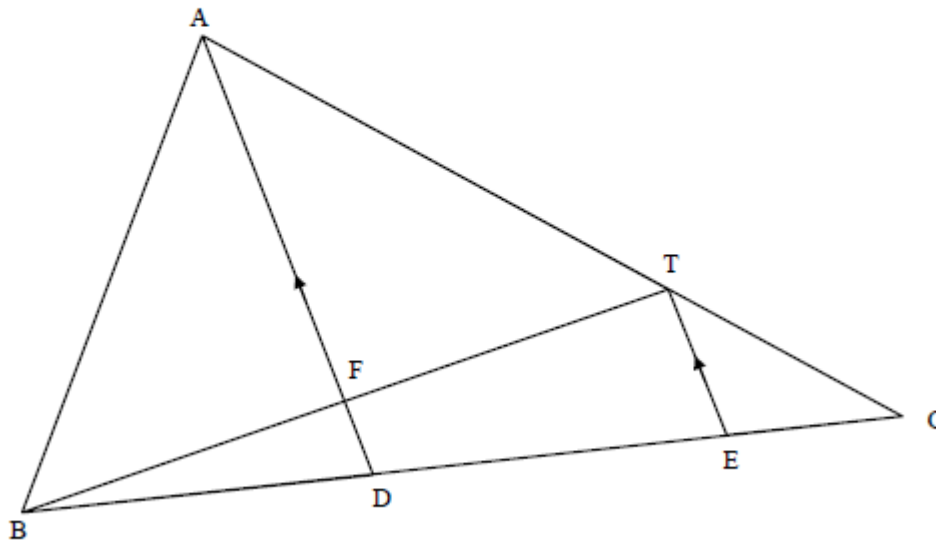


- 9.1 Why is  $\hat{PRQ} = 90^\circ$ ? (1)
- 9.2 Prove that  $\hat{P}_1 = \hat{S}$ . (3)
- 9.3 Prove that SRWT is a cyclic quadrilateral. (3)
- 9.4 Prove that  $\triangle QWR \parallel \triangle QST$ . (3)
- 9.5 If  $QW = 5$  cm,  $TW = 3$  cm,  $QR = 4$  cm and  $WR = 2$  cm, calculate the length of:
- 9.5.1 TS (3)
- 9.5.2 SR (3)
- [16]**

## EUCLIDEAN GEOMETRY: GRADE 12

### QUESTION 10

In the figure below,  $\triangle ABC$  has D and E on BC.  $BD = 6$  cm and  $DC = 9$  cm.  
 $AT : TC = 2 : 1$  and  $AD \parallel TE$ .



- 10.1 Write down the numerical value of  $\frac{CE}{ED}$  (1)
- 10.2 Show that D is the midpoint of BE. (2)
- 10.3 If  $FD = 2$  cm, calculate the length of TE. (2)
- 10.4 Calculate the numerical value of:
- 10.4.1  $\frac{\text{Area of } \triangle ADC}{\text{Area of } \triangle ABD}$  (1)
- 10.4.2  $\frac{\text{Area of } \triangle TEC}{\text{Area of } \triangle ABC}$  (3)

[9]

**EUCLIDEAN GEOMETRY: GRADE 12**

**FEBRUARY - MARCH 2009**

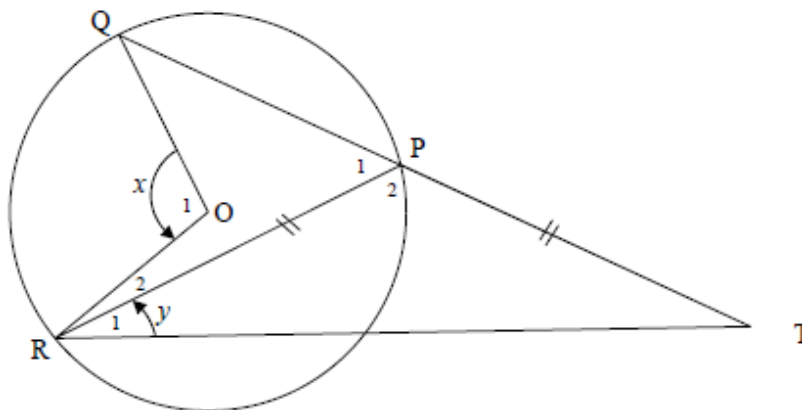
**QUESTION 6**

6.1 Complete the statement below by filling in the missing word(s) so that the statement is CORRECT:

The angle subtended by a chord or arc at the centre of a circle is ... (1)

6.2 In the figure below, O is the centre of the circle and  $PT = PR$ .

Let  $\hat{R}_1 = y$  and  $\hat{O}_1 = x$ .



6.2.1 Express  $x$  in terms of  $y$ . (3)

6.2.2 If  $TQ = TR$  and  $x = 120^\circ$ , calculate the measure of:

(a)  $y$  (2)

(b)  $\hat{R}_2$  (Hint: Draw QR) (3)

[9]

## EUCLIDEAN GEOMETRY: GRADE 12

NOVEMBER 2009

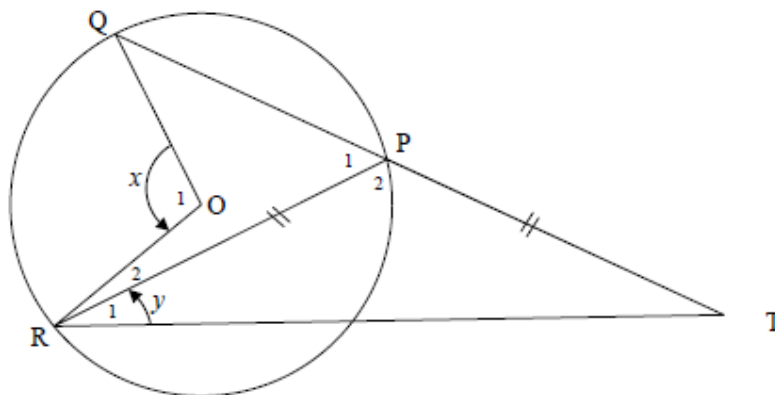
### QUESTION 6

6.1 Complete the statement below by filling in the missing word(s) so that the statement is CORRECT:

The angle subtended by a chord or arc at the centre of a circle is ... (1)

6.2 In the figure below, O is the centre of the circle and  $PT = PR$ .

Let  $\hat{R}_1 = y$  and  $\hat{O}_1 = x$ .



6.2.1 Express  $x$  in terms of  $y$ . (3)

6.2.2 If  $TQ = TR$  and  $x = 120^\circ$ , calculate the measure of:

(a)  $y$  (2)

(b)  $\hat{R}_2$  (Hint: Draw QR) (3)

[9]

**EUCLIDEAN GEOMETRY: GRADE 12**

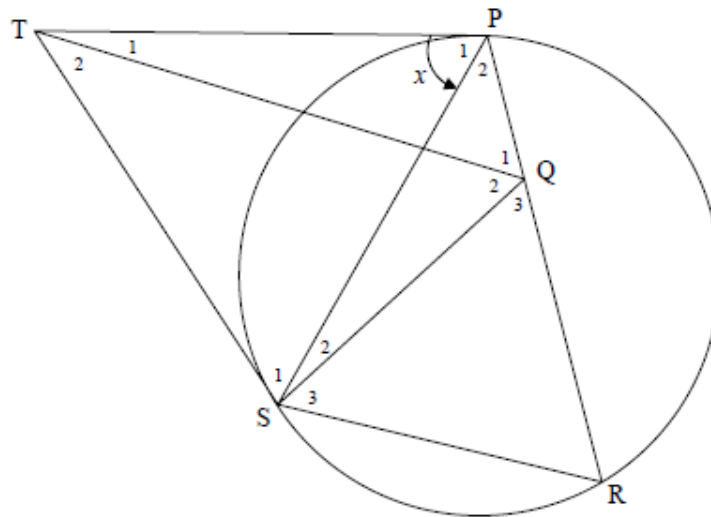
**QUESTION 7**

In the figure TP and TS are tangents to the given circle. R is a point on the circumference.

Q is a point on PR such that  $\hat{Q}_1 = \hat{P}_1$ .

SQ is drawn.

Let  $\hat{P}_1 = x$ .



Prove that:

7.1  $TQ \parallel SR$  (4)

7.2 QPTS is a cyclic quadrilateral (4)

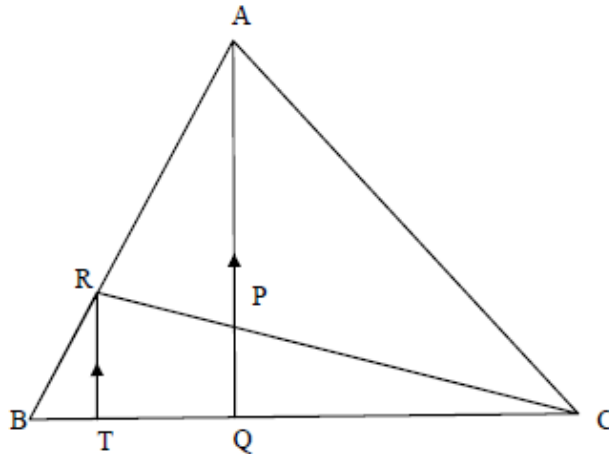
7.3 TQ bisects  $\hat{SQP}$  (3)

[11]

**EUCLIDEAN GEOMETRY: GRADE 12**

**QUESTION 8**

In the figure  $AQ \parallel RT$ ,  $\frac{BQ}{QC} = \frac{3}{5}$  and  $\frac{BR}{RA} = \frac{1}{2}$ .



8.1 If  $BT = k$ , calculate  $TQ$  in terms of  $k$ . (3)

8.2 Hence, or otherwise, calculate the numerical value of:

8.2.1  $\frac{CP}{PR}$  (3)

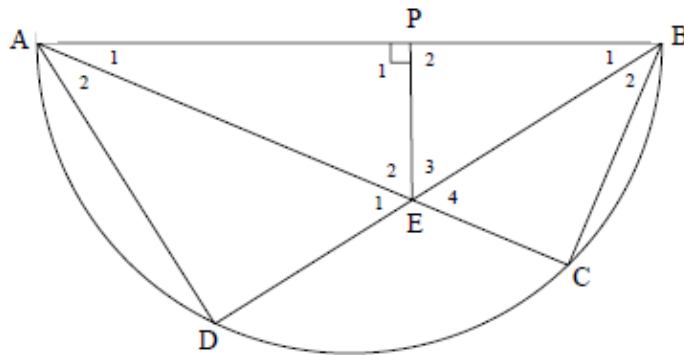
8.2.2  $\frac{\text{Area } \Delta RCT}{\text{Area } \Delta ABC}$  (4)  
[10]



## EUCLIDEAN GEOMETRY: GRADE 12

### QUESTION 9

In the accompanying figure,  $AB$  is the diameter of circle  $ADCB$ . Chords  $AC$  and  $BD$  intersect at  $E$ .  $EP$  is perpendicular to  $AB$ .



- 9.1 Prove that  $\triangle BPE \sim \triangle BDA$ . (3)
- 9.2 Hence show that  $\frac{BP}{BD} = \frac{PE}{AD}$ . (2)
- 9.3 Prove that  $AB^2 = BD^2 + \frac{BD^2 \cdot PE^2}{BP^2}$ . (5)
- [10]**

**EUCLIDEAN GEOMETRY: GRADE 12**

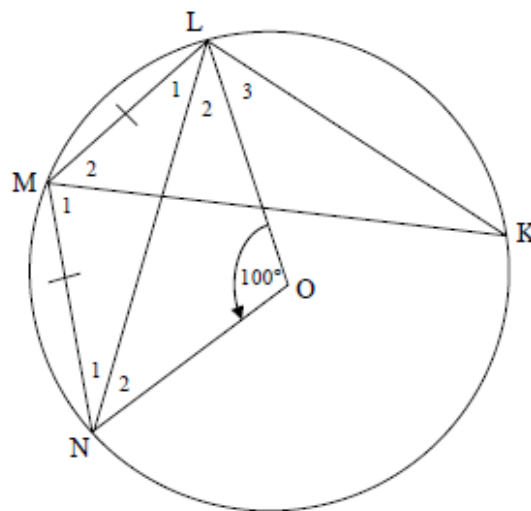
**FEBRUARY - MARCH 2010**

**QUESTION 8**

8.1 Complete the statement:

The sum of the angles around a point is ... (1)

8.2 In the figure below, O is the centre of the circle. K, L, M and N are points on the circumference of the circle such that  $LM = MN$ .  $\hat{LON} = 100^\circ$ .



Determine, with reasons, the values of the following:

8.2.1  $\hat{LMN}$  (3)

8.2.2  $\hat{LKM}$  (3)  
[7]

**EUCLIDEAN GEOMETRY: GRADE 12**

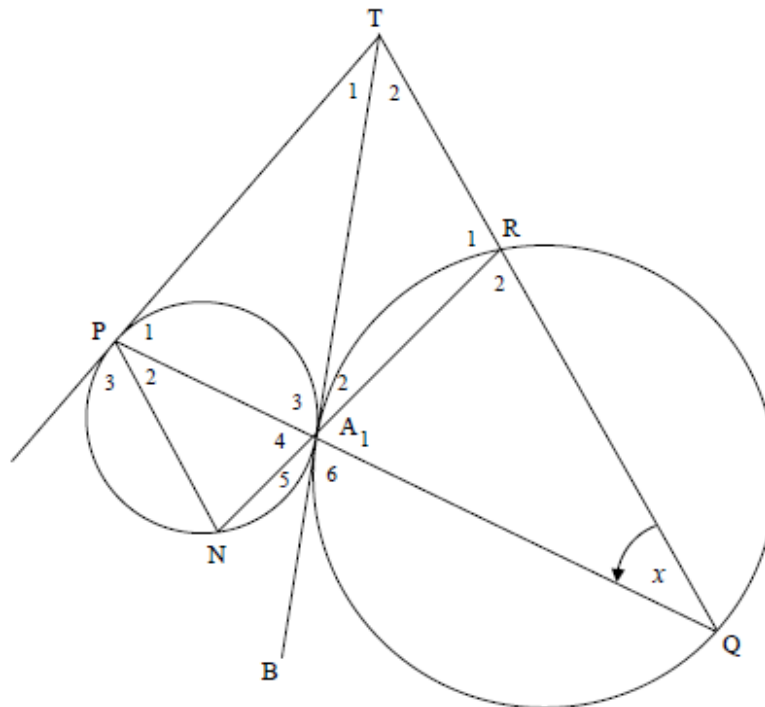
**QUESTION 9**

9.1 Complete the following statement:

The angle between the tangent and the chord ... (1)

9.2 In the diagram below, two circles have a common tangent TAB. PT is a tangent to the smaller circle. PAQ, QRT and NAR are straight lines.

Let  $\hat{Q} = x$ .



9.2.1 Name, with reasons, THREE other angles equal to  $x$ . (5)

9.2.2 Prove that APTR is a cyclic quadrilateral. (5)

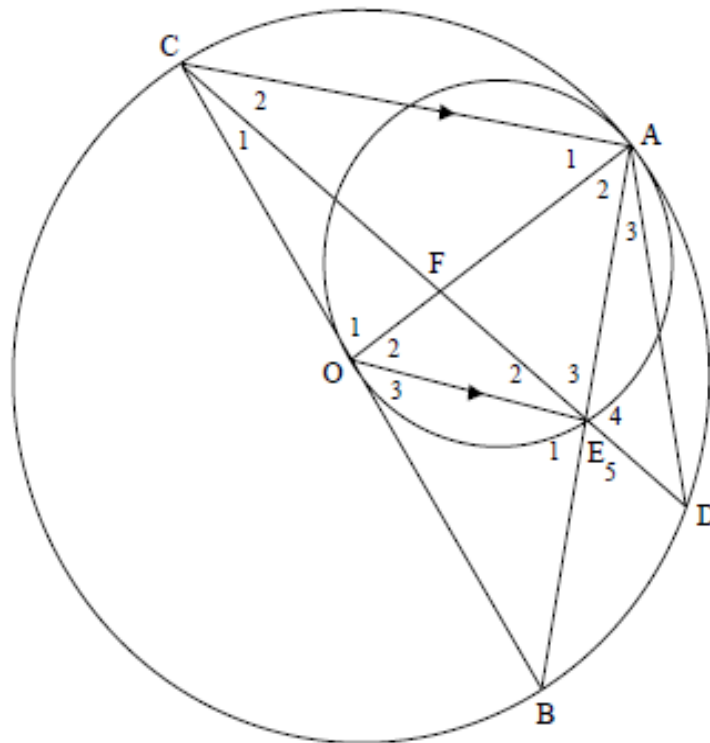
[11]

**EUCLIDEAN GEOMETRY: GRADE 12**

**QUESTION 10**

Two circles touch each other at point A. The smaller circle passes through O, the centre of the larger circle. Point E is on the circumference of the smaller circle. A, D, B and C are points on the circumference of the larger circle. OE  $\parallel$  CA.

OE  $\parallel$  CA.



- 10.1 Prove, with reasons, that  $AE = BE$ . (2)
  - 10.2 Prove that  $\triangle AED \parallel \triangle CEB$ . (3)
  - 10.3 Hence, or otherwise, show that  $AE^2 = DE \cdot CE$ . (2)
  - 10.4 If  $AE \cdot EB = EF \cdot EC$ , show that E is the midpoint of DF. (3)
- [10]**

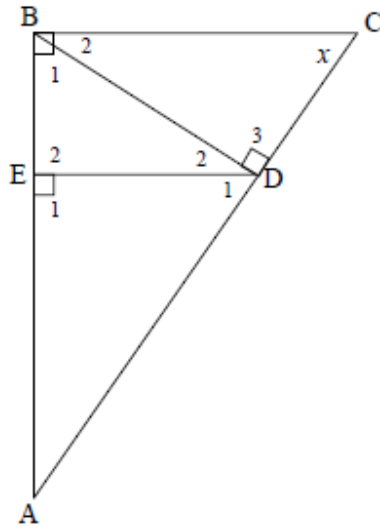
## EUCLIDEAN GEOMETRY: GRADE 12

### QUESTION 11

$\triangle ABC$  is a right-angled triangle with  $\hat{B} = 90^\circ$ . D is a point on AC such that  $BD \perp AC$  and E is a point on AB such that  $DE \perp AB$ . E and D are joined.

$AD : DC = 3 : 2$ .

$AD = 15$  cm.



- 11.1 Prove that  $\triangle BDA \sim \triangle CDB$ . (3)
- 11.2 Calculate BD (Leave your answer in surd form). (3)
- 11.3 Calculate AE (Leave your answer in surd form). (6)
- [12]**

**EUCLIDEAN GEOMETRY: GRADE 12**

NOVEMBER 2010

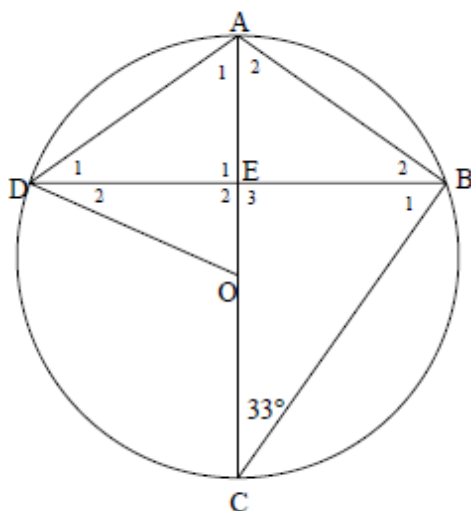
**QUESTION 6**

Given:  $T_{k+1} = T_k + (5 - 4k)$  where  $T_1 = 3$  and  $k \geq 1$

- 6.1 Determine the FIRST FOUR terms of the sequence. (3)
- 6.2 What type of sequence will this formula generate? Give a reason for your answer. (2)  
[5]

**QUESTION 7**

In the diagram below AC is a diameter of the circle with centre O. AC and chord BD intersect at E. AB, BC and AD are also chords of the circle. OD is joined.  $AE \perp BD$ .



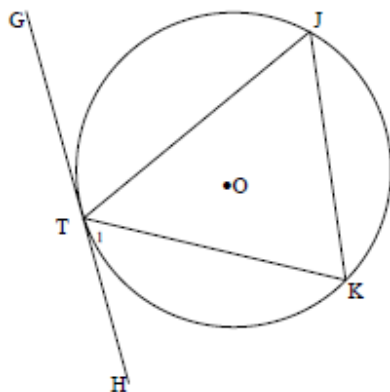
If  $\hat{C} = 33^\circ$ , calculate, with reasons, the size of:

- 7.1  $\hat{A}_1$  (3)
- 7.2  $\hat{D}_2$  (2)
- 7.3 Show that AE bisects  $\hat{DAB}$  (3)  
[8]

**EUCLIDEAN GEOMETRY: GRADE 12**

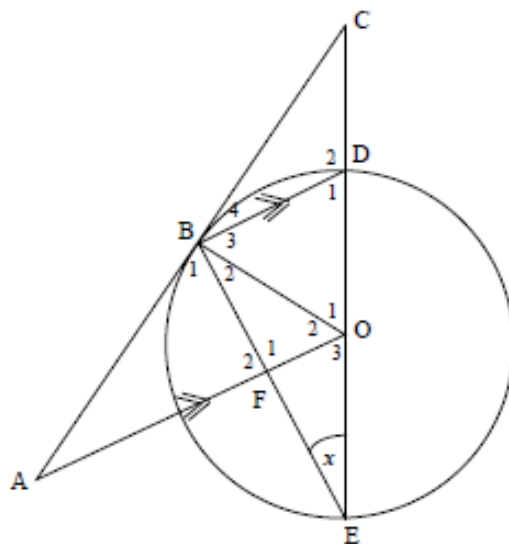
**QUESTION 8**

- 8.1 In the diagram below O is the centre of the circle. GH is a tangent to the circle at T. J and K are points on the circumference of the circle. TJ, TK and JK are joined.



Prove the theorem that states  $\hat{T}_1 = \hat{TJK}$ . (5)

- 8.2 ED is a diameter of the circle, with centre O. ED is extended to C. CA is a tangent to the circle at B. AO intersects BE at F.  $BD \parallel AO$ .  $\hat{E} = x$ .



- 8.2.1 Write down, with reasons, THREE other angles equal to  $x$ . (4)
- 8.2.2 Determine, with reasons,  $\hat{CBE}$  in terms of  $x$ . (3)
- 8.2.3 Prove that F is the midpoint of BE. (4)
- 8.2.4 Prove that  $\triangle CBD \parallel \triangle CEB$ . (2)
- 8.2.5 Prove that  $2EF \cdot CB = CE \cdot BD$ . (3)
- [21]**

**EUCLIDEAN GEOMETRY: GRADE 12**

**QUESTION 9**

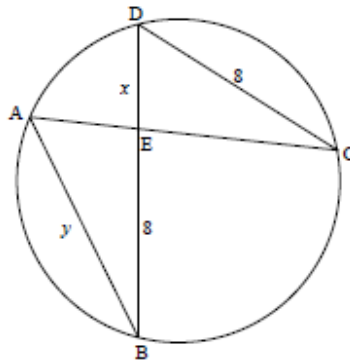
In the diagram below A, B, C and D are points on the circumference of the circle.

BD and AC intersect at E. Also,

EB = 8 cm,

DC = 8 cm and

AE : EC = 4 : 7.

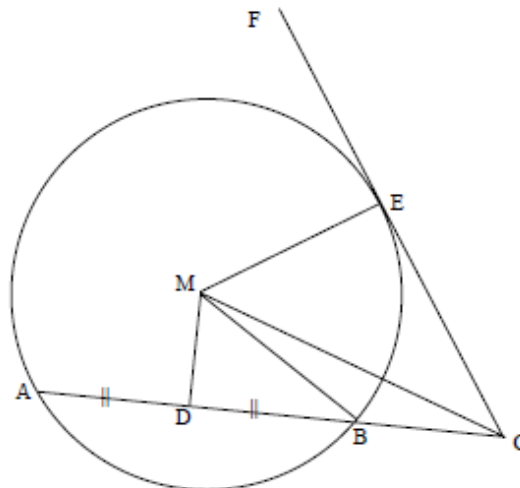


If  $DE = x$  units and  $AB = y$  units, calculate  $x$  and  $y$ .

[6]

**QUESTION 10**

In the diagram below M is the centre of the circle. FEC is a tangent to the circle at E. D is the midpoint of AB.



10.1 Prove MDCE is a cyclic quadrilateral. (3)

10.2 Prove that  $MC^2 = MB^2 + DC^2 - DB^2$ . (3)

10.3 Calculate CE if  $AB = 60$  mm,  $ME = 40$  mm and  $BC = 20$  mm. (4)

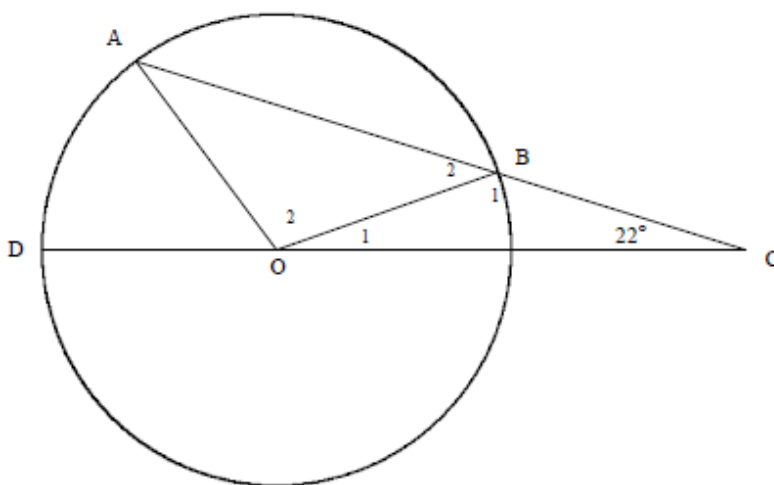
[10]



**FEBRUARY - MARCH 2011**

**QUESTION 8**

O is the centre of the circle. AB produced and DO produced meet at C.  
 $BC = OA$  and  $\hat{A}CO = 22^\circ$ .



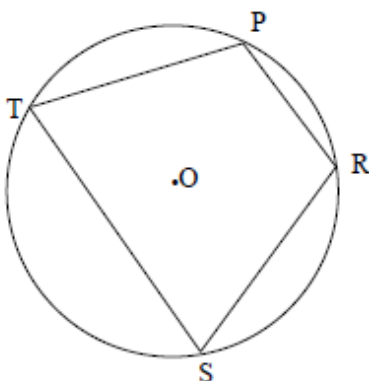
Calculate, with reasons,  $\hat{A}OD$ .

[5]

**QUESTION 9**

9.1 In the figure below O is the centre of the circle and PRST is a cyclic quadrilateral.

Prove the theorem that states  $\hat{P}RS + \hat{P}TS = 180^\circ$ .



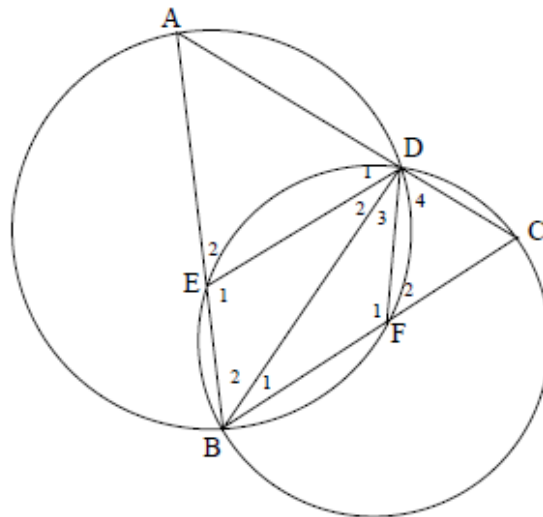
(5)

**EUCLIDEAN GEOMETRY: GRADE 12**

- 9.2 In the diagram below two circles intersect one another at D and B. AB is a straight line such that it intersects the circle BCD at point E. BC is a straight line such that it intersects the circle ABD at F. DE, DB and DF are joined.

$$\hat{F}_2 = 180^\circ - 2x$$

$$FC = FD$$



- 9.2.1 Calculate, with reasons, in terms of  $x$ :
- (a)  $\hat{D}_E B$  (3)
- (b)  $\hat{A}$  (2)
- 9.2.2 Hence, or otherwise, prove  $ED \parallel BC$ . (3)
- [13]**

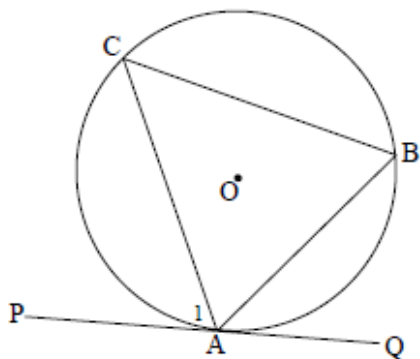
**EUCLIDEAN GEOMETRY: GRADE 12**

NOVEMBER 2011

**QUESTION 8**

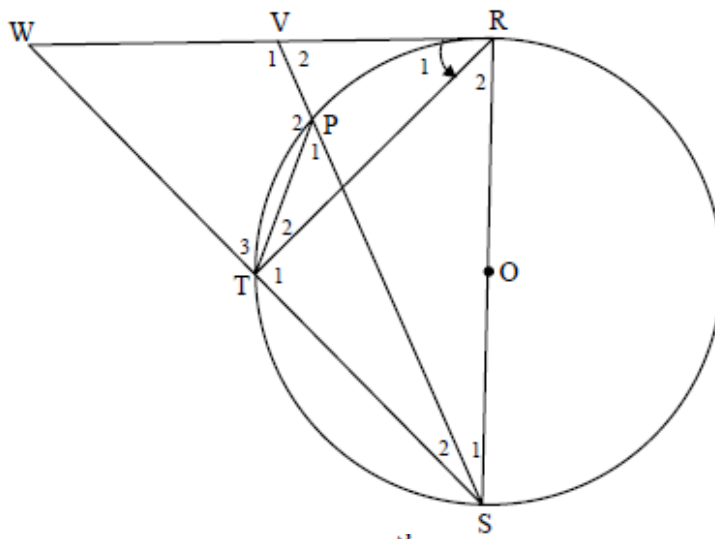
- 8.1 In the diagram below,  $O$  is the centre of the circle.  $PQ$  is a tangent to the circle at  $A$ .  $B$  and  $C$  are points on the circumference of the circle.  $AB$ ,  $AC$  and  $BC$  are joined.

Prove the theorem that states  $\hat{C}AP = \hat{A}BC$ .



(5)

- 8.2  $RS$  is a diameter of the circle with centre  $O$ . Chord  $ST$  is produced to  $W$ . Chord  $SP$  produced meets the tangent  $RW$  at  $V$ .  $\hat{R}_1 = 50^\circ$ .



Calculate the size of:

8.2.1  $\hat{W}RS$  (1)

8.2.2  $\hat{W}$  (2)

8.2.3  $\hat{P}_1$  (3)

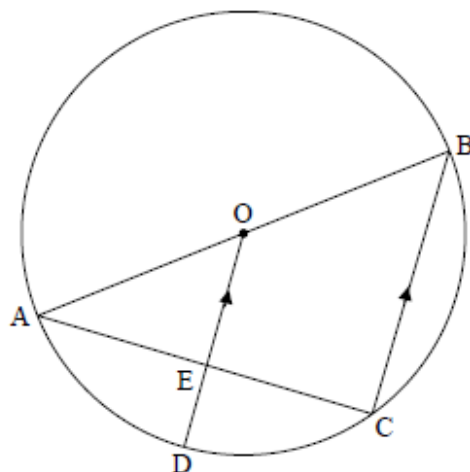
8.2.4 Prove that  $\hat{V}_1 = \hat{P}TS$ . (4)

[15]

**EUCLIDEAN GEOMETRY: GRADE 12**

**QUESTION 9**

AB is a diameter of the circle ABCD. OD is drawn parallel to BC and meets AC in E.

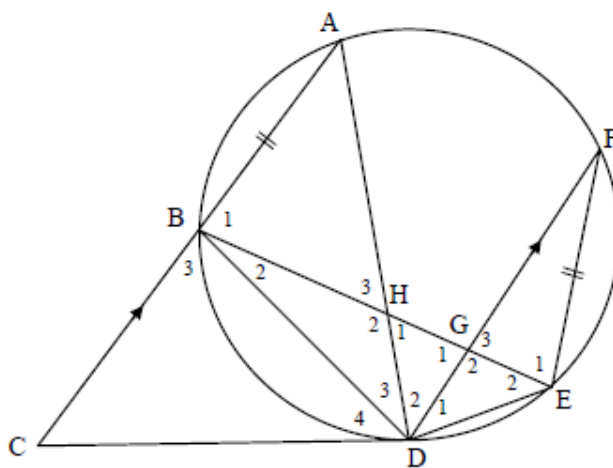


If the radius is 10 cm and  $AC = 16$  cm, calculate the length of ED.

[5]

**QUESTION 10**

CD is a tangent to circle ABDEF at D. Chord AB is produced to C. Chord BE cuts chord AD in H and chord FD in G.  $AC \parallel FD$  and  $FE = AB$ . Let  $\hat{D}_4 = x$  and  $\hat{D}_1 = y$ .



10.1 Determine THREE other angles that are each equal to  $x$ .

(6)

10.2 Prove that  $\triangle BHD \parallel \triangle FED$ .

(5)

10.3 Hence, or otherwise, prove that  $AB \cdot BD = FD \cdot BH$ .

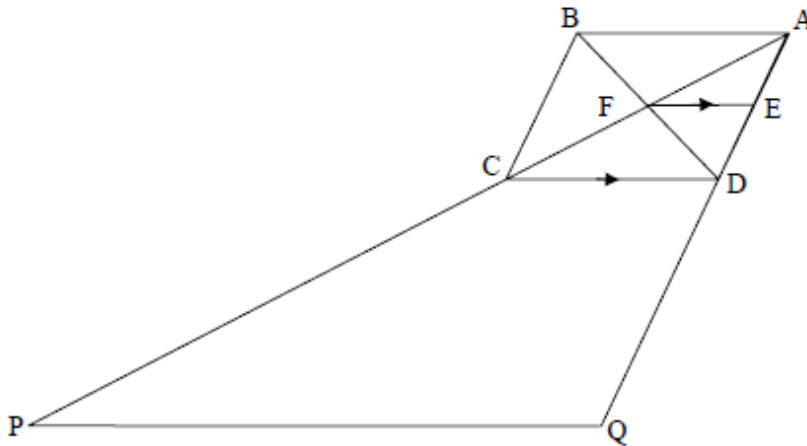
(2)

[13]

**EUCLIDEAN GEOMETRY: GRADE 12**

**QUESTION 11**

ABCD is a parallelogram with diagonals intersecting at F. FE is drawn parallel to CD. AC is produced to P such that  $PC = 2AC$  and AD is produced to Q such that  $DQ = 2AD$ .



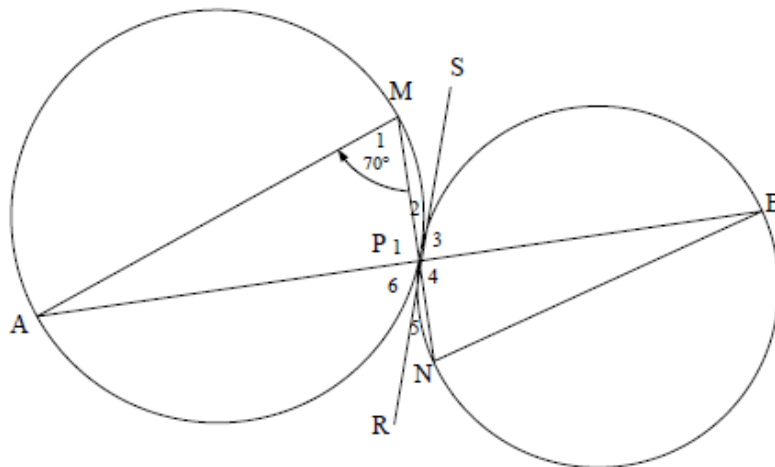
- 11.1 Show that E is the midpoint of AD. (2)
- 11.2 Prove  $PQ \parallel FE$ . (3)
- 11.3 If PQ is 60 cm, calculate the length of FE. (5)
- [10]**

**EUCLIDEAN GEOMETRY: GRADE 12**

**FEBRUARY - MARCH 2012**

**QUESTION 8**

In the diagram below,  $AM$  is the diameter of the bigger circle  $AMP$ .  $RPS$  is a common tangent to both circles at  $P$ .  $APB$  and  $MPN$  are straight lines.



- 8.1 State the size of  $\hat{P}_1$ . (1)
- 8.2 Hence, show that  $BN$  is the diameter of the smaller circle. (2)
- 8.3 If  $\hat{M}_1 = 70^\circ$ , calculate the size of each of the following angles:
- 8.3.1  $\hat{A}$  (1)
- 8.3.2  $\hat{P}_6$  (1)
- 8.3.3  $\hat{B}$  (2)
- [7]

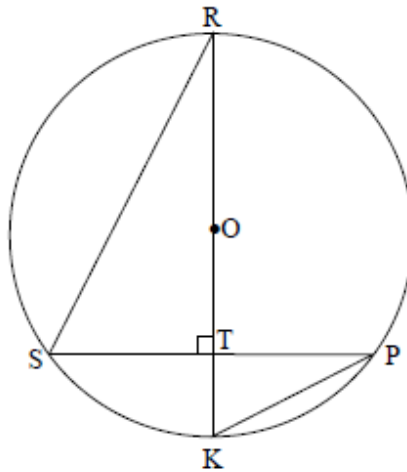
**EUCLIDEAN GEOMETRY: GRADE 12**

**QUESTION 9**

In the diagram below,  $O$  is the centre of the circle with diameter  $RK$ .

$PS \perp RK$

$RK$  intersects  $PS$  at  $T$ .



- 9.1 If  $PS = 4x$ , write down the length of  $ST$  in terms of  $x$ . (1)
- 9.2 Prove that  $\triangle RST \cong \triangle PKT$ . (3)
- 9.3 If it is further given that  $TK = x$  and  $RT = 320$  mm, calculate the value of  $x$ . (3)
- [7]

## EUCLIDEAN GEOMETRY: GRADE 12

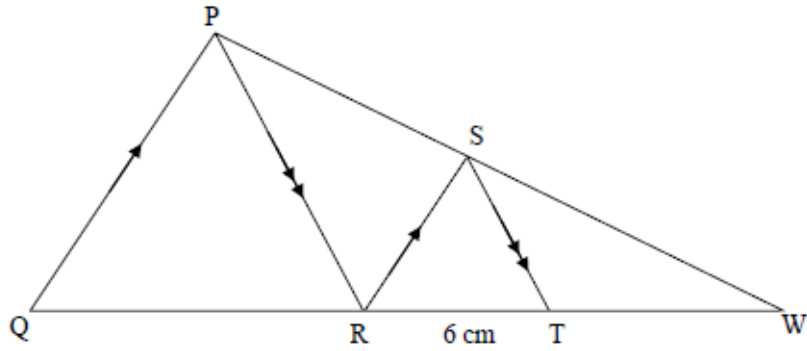
### QUESTION 10

In  $\triangle PQW$ ,  $S$  is a point on  $PW$  and  $R$  is a point on  $QW$  such that  $SR \parallel PQ$ .

$T$  is a point on  $QW$  such that  $ST \parallel PR$ .

$RT = 6$  cm

$WS : SP = 3 : 2$



Calculate:

10.1 WT

(3)

10.2 WQ

(4)

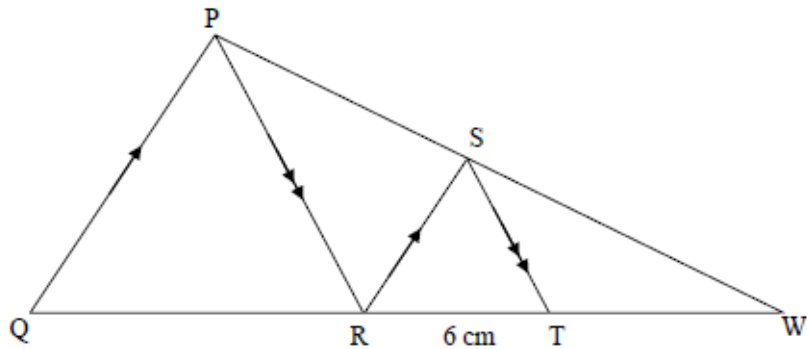
[7]



**EUCLIDEAN GEOMETRY: GRADE 12**

**QUESTION 10**

In  $\triangle PQW$ ,  $S$  is a point on  $PW$  and  $R$  is a point on  $QW$  such that  $SR \parallel PQ$ .  
 $T$  is a point on  $QW$  such that  $ST \parallel PR$ .  
 $RT = 6$  cm  
 $WS : SP = 3 : 2$



Calculate:

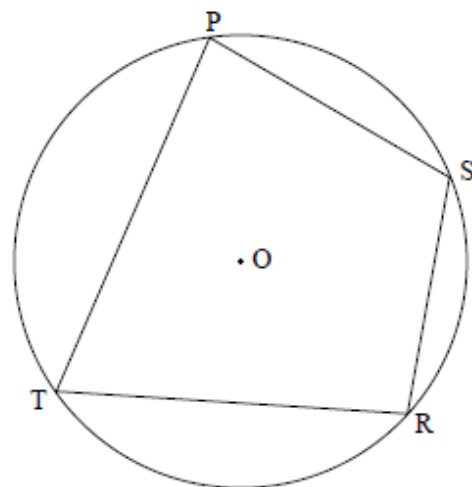
10.1  $WT$  (3)

10.2  $WQ$  (4)

[7]

**QUESTION 11**

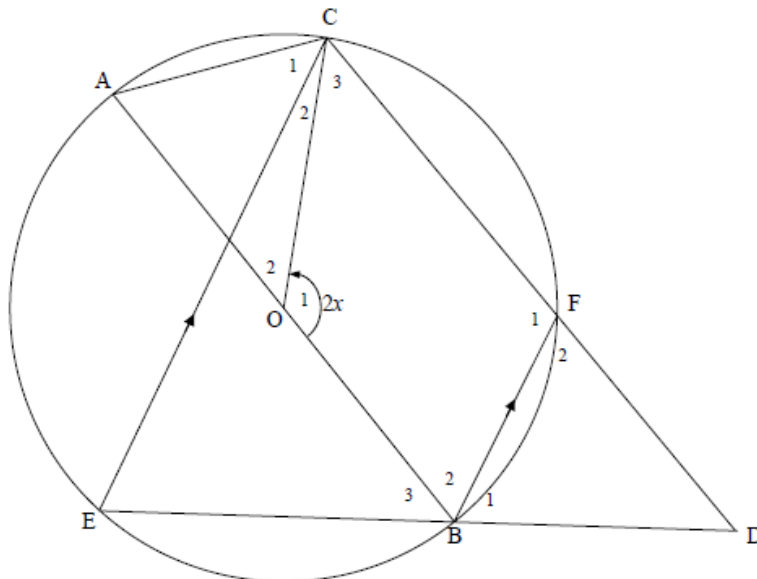
11.1 In the diagram below,  $O$  is the centre of the circle.  $PSRT$  is a cyclic quadrilateral. Prove the theorem that states  $\hat{PTR} + \hat{PSR} = 180^\circ$ .



(6)

## EUCLIDEAN GEOMETRY: GRADE 12

- 11.2 In the diagram below,  $O$  is the centre of the circle.  $AB$  is a diameter of the circle. Chord  $CF$  produced meets chord  $EB$  produced at  $D$ . Chord  $EC$  is parallel to chord  $BF$ .  $CO$  and  $AC$  are joined. Let  $\hat{O}_1 = 2x$

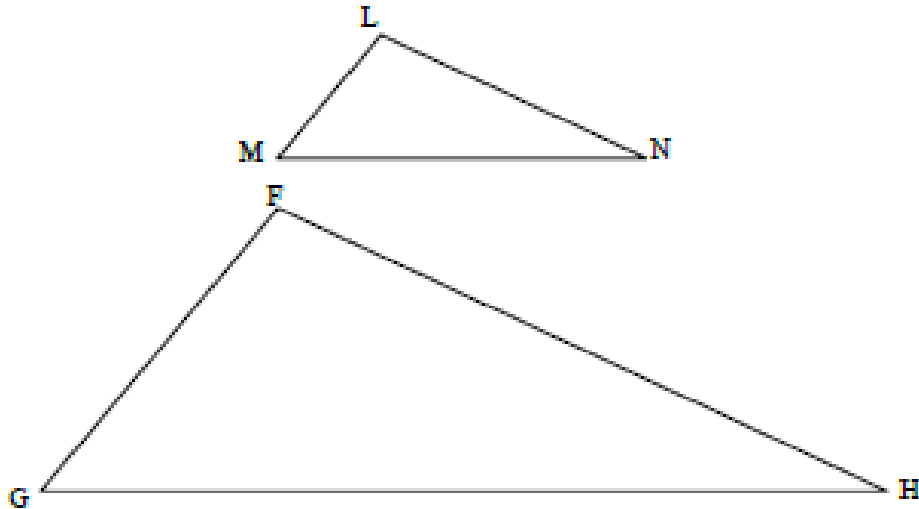


- 11.2.1 Determine, in terms of  $x$ , the size of  $\hat{F}_1$ . (4)
- 11.2.2 Prove that  $DF = BD$ . (4)
- 11.2.3 Show that  $\hat{C}_1 = \hat{C}_3$ . (4)
- 11.2.4 If  $DF = 5$  cm and  $OA = 6$  cm, calculate area  $\triangle BFD$  : area  $\triangle AOC$ . (4)
- [22]

NOVEMBER 2012

**QUESTION 7**

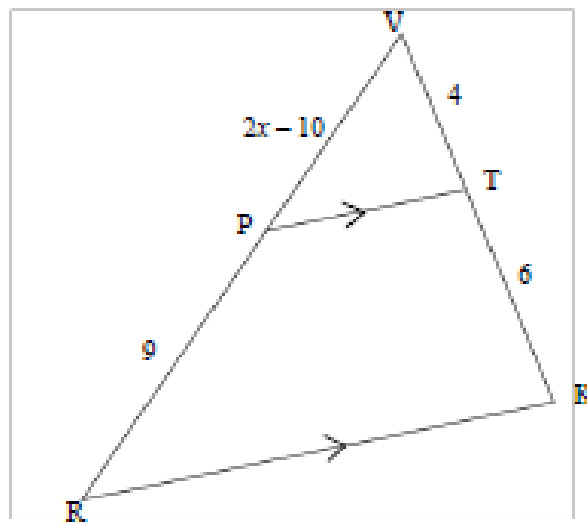
- 7.1 If in  $\triangle LMN$  and  $\triangle FGH$  it is given that  $\hat{L} = \hat{F}$  and  $\hat{M} = \hat{G}$ , prove the theorem that states  $\frac{LM}{FG} = \frac{LN}{FH}$ .



(7)

- 7.2 In the diagram below,  $\triangle VRK$  has P on VR and T on VK such that  $PT \parallel RK$ .  $VT = 4$  units,  $PR = 9$  units,  $TK = 6$  units and  $VP = 2x - 10$  units.

Calculate the value of  $x$ .



(4)  
[11]

## EUCLIDEAN GEOMETRY: GRADE 12

### QUESTION 8

8.1 Complete the following statement:

The angle between the tangent and the chord is equal ... (1)

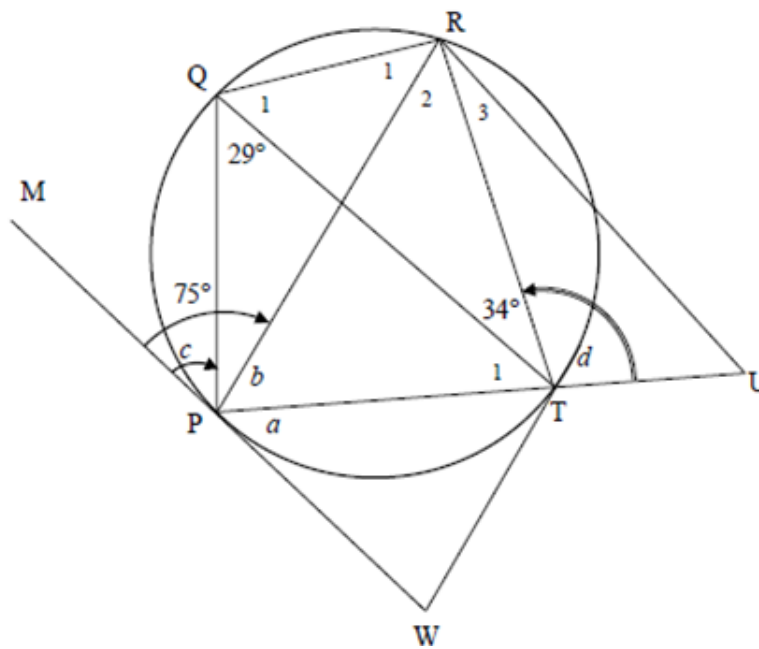
8.2 In the diagram points P, Q, R and T lie on the circumference of a circle. MW and TW are tangents to the circle at P and T respectively. PT is produced to meet RU at U.

$$\hat{M}PR = 75^\circ$$

$$\hat{P}QT = 29^\circ$$

$$\hat{Q}TR = 34^\circ$$

Let  $\hat{TPW} = a$ ,  $\hat{RPT} = b$ ,  $\hat{MPQ} = c$  and  $\hat{RTU} = d$ , calculate the values of  $a$ ,  $b$ ,  $c$  and  $d$ .

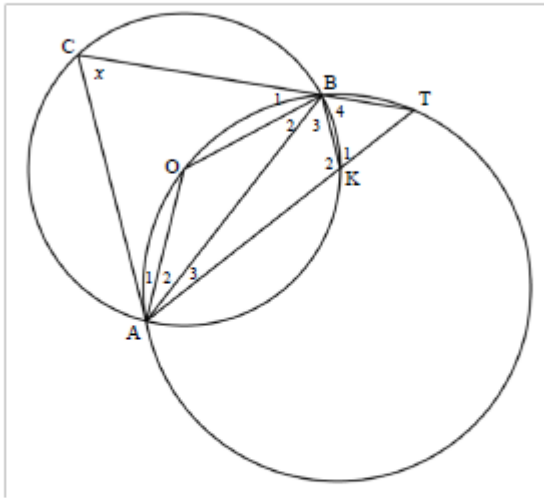


(9)  
[10]

## EUCLIDEAN GEOMETRY: GRADE 12

### QUESTION 9

O is the centre of the circle CAKB.  
 AK produced intersects circle AOBT at T.  
 $\hat{ACB} = x$

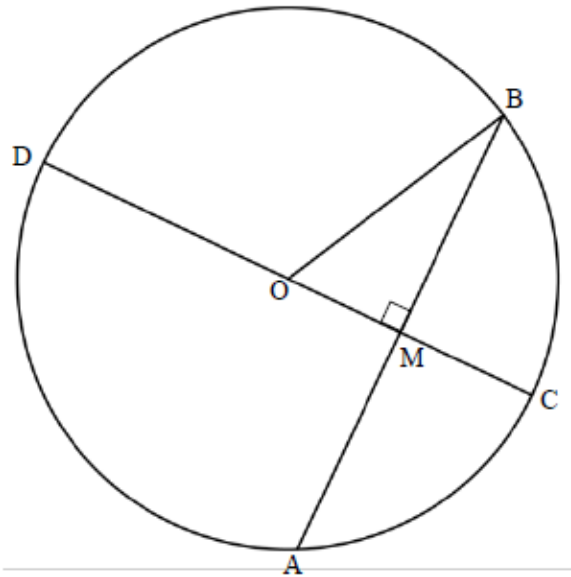


- 9.1 Prove that  $\hat{T} = 180^\circ - 2x$ . (3)
- 9.2 Prove  $AC \parallel KB$ . (5)
- 9.3 Prove  $\triangle BKT \parallel \triangle CAT$ . (3)
- 9.4 If  $AK : KT = 5 : 2$ , determine the value of  $\frac{AC}{KB}$ . (3)
- [14]

## EUCLIDEAN GEOMETRY: GRADE 12

### QUESTION 10

In the diagram below,  $O$  is the centre of the circle. Chord  $AB$  is perpendicular to diameter  $DC$ .  
 $CM : MD = 4 : 9$  and  $AB = 24$  units.



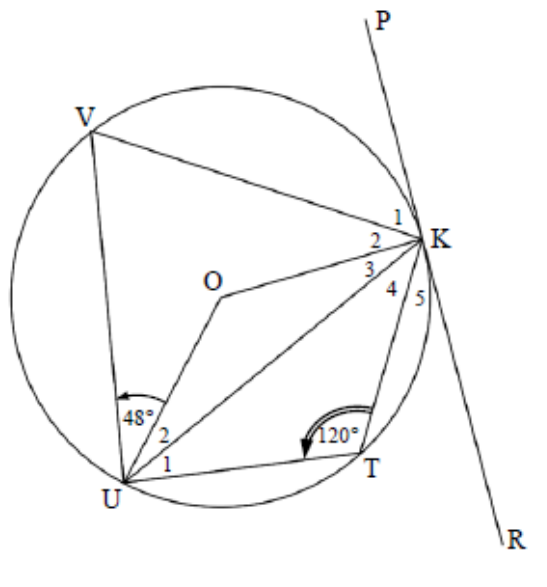
- 10.1 Determine an expression for  $DC$  in terms of  $x$  if  $CM = 4x$  units. (1)
- 10.2 Determine an expression for  $OM$  in terms of  $x$ . (2)
- 10.3 Hence, or otherwise, calculate the length of the radius. (4)
- [7]

## EUCLIDEAN GEOMETRY: GRADE 12

FEBRUARY - MARCH 2013

### QUESTION 8

In the diagram below,  $O$  is the centre of the circle  $KTUV$ .  $PKR$  is a tangent to the circle at  $K$ .  $\hat{O}UV = 48^\circ$  and  $\hat{K}TU = 120^\circ$ .



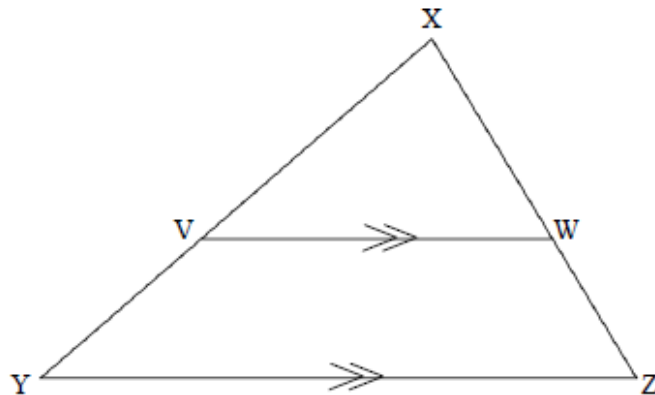
Calculate, with reasons, the sizes of the following angles:

- |     |             |             |
|-----|-------------|-------------|
| 8.1 | $\hat{V}$   | (2)         |
| 8.2 | $\hat{K}OU$ | (2)         |
| 8.3 | $\hat{U}_2$ | (2)         |
| 8.4 | $\hat{K}_1$ | (2)         |
| 8.5 | $\hat{K}_2$ | (2)         |
|     |             | <b>[10]</b> |

## EUCLIDEAN GEOMETRY: GRADE 12

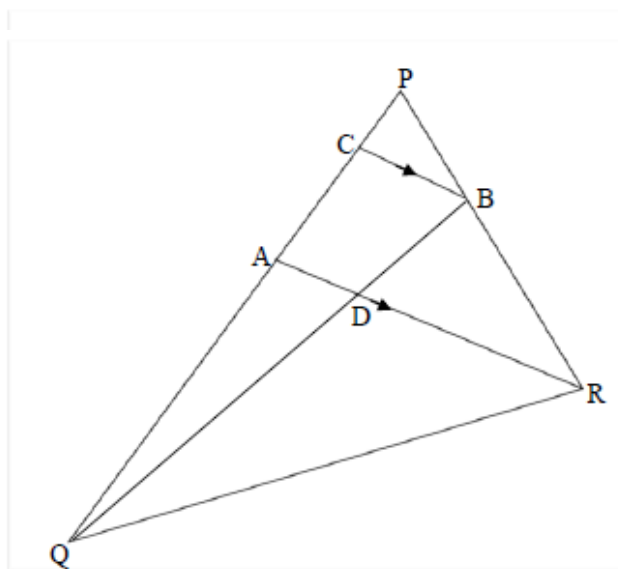
### QUESTION 9

- 9.1 Use the diagram below to prove the theorem which states that if  $VW \parallel YZ$  then  $\frac{XV}{VY} = \frac{XW}{WZ}$ .



(6)

- 9.2 In  $\triangle PQR$  below, B lies on PR such that  $2PB = BR$ . A lies on PQ such that  $PA : AQ = 3 : 8$ . BC is drawn parallel to AR.



- 9.2.1 Write down the value of  $\frac{\text{area of } \triangle PRA}{\text{area of } \triangle QRA}$  (2)

- 9.2.2 Calculate the value of the ratio  $\frac{BD}{BQ}$ . Show all working to support your answer. (5)

[13]

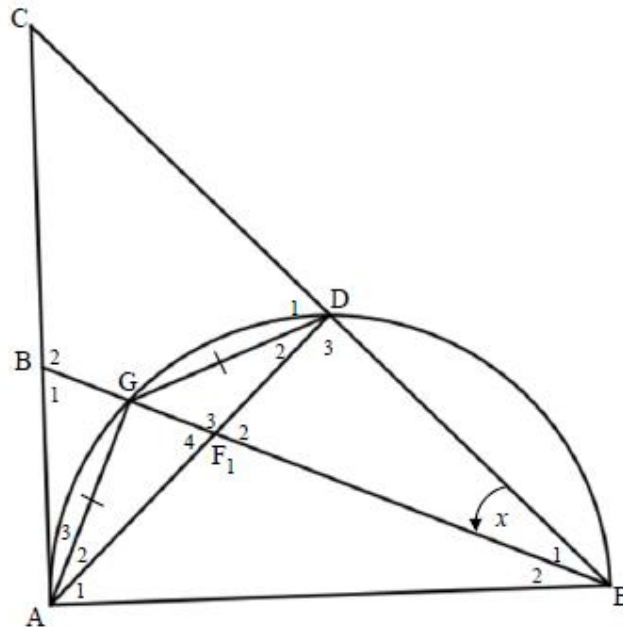


**EUCLIDEAN GEOMETRY: GRADE 12**

**QUESTION 10**

In the figure AGDE is a semicircle. AC is the tangent to the semicircle at A and EG produced intersects AC at B. AD intersects BE in F.

AG = GD.  $\hat{E}_1 = x$ .



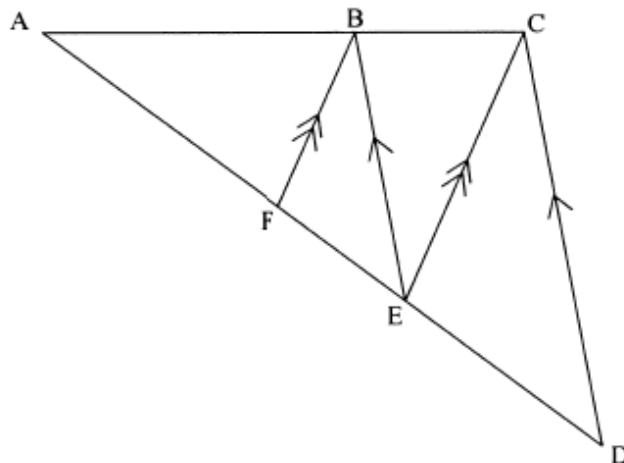
- 10.1 Write down, with reasons, FOUR other angles each equal to  $x$ . (8)
- 10.2 Prove that  $BE \cdot DE = AE \cdot FE$  (7)
- 10.3 Prove that  $\hat{B}_1 = \hat{D}_1$  (4)
- [19]**

**EUCLIDEAN GEOMETRY: GRADE 12**

**NOVEMBER 2013**

**QUESTION 9**

In  $\triangle ADC$ , E is a point on AD and B is a point on AC such that  $EB \parallel DC$ .  
F is a point on AD such that  $FB \parallel EC$ . It is also given that  $AB = 2BC$ .



9.1 Determine the value of  $AF : FE$  (2)

9.2 Calculate the length of ED if  $AF = 8$  cm. (4)

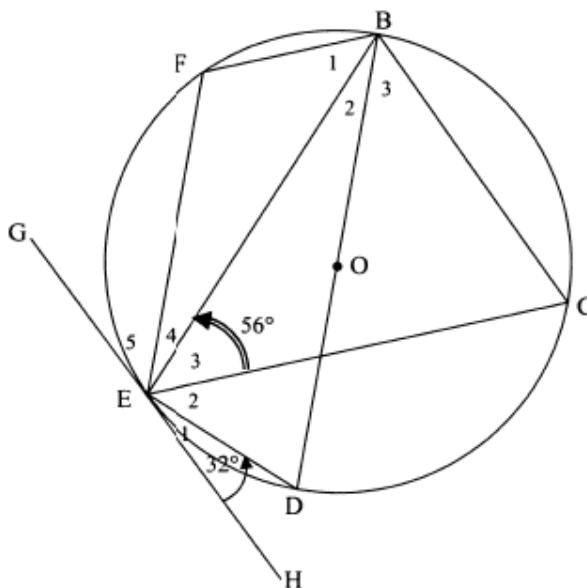
**[6]**

**EUCLIDEAN GEOMETRY: GRADE 12**

**QUESTION 10**

In the diagram below,  $O$  is the centre of the circle.  $BD$  is a diameter of the circle.  $GEH$  is a tangent to the circle at  $E$ .  $F$  and  $C$  are two points on the circle and  $FB$ ,  $FE$ ,  $BC$ ,  $CE$  and  $BE$  are drawn.

$\hat{E}_1 = 32^\circ$  and  $\hat{E}_3 = 56^\circ$ .



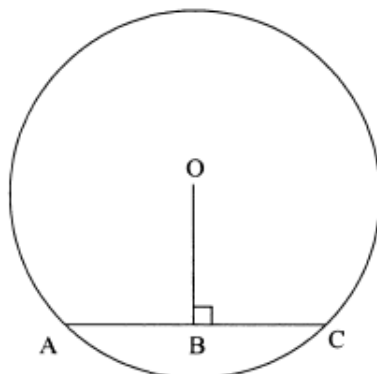
Calculate, with reasons, the values of:

- 10.1  $\hat{E}_2$  (2)
  - 10.2  $\hat{E}BC$  (3)
  - 10.3  $\hat{F}$  (4)
- [9]**

**QUESTION 11**

In the diagram below,  $O$  is the centre of the circle and  $OB$  is perpendicular to the chord  $AC$ .

Prove, using Euclidean geometry methods, the theorem that states  $AB = BC$ .



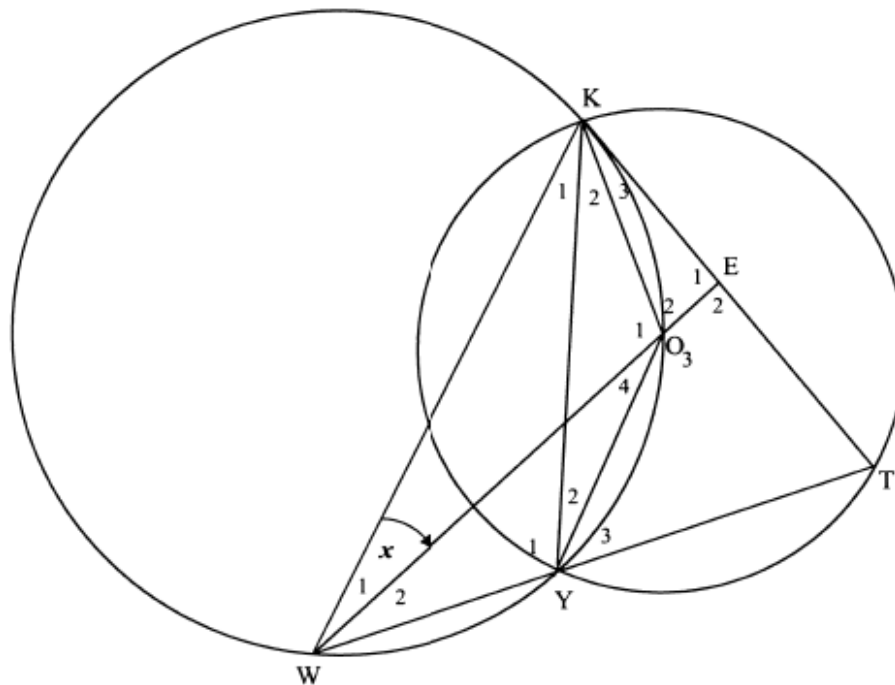
**[5]**

**EUCLIDEAN GEOMETRY: GRADE 12**

**QUESTION 12**

In the diagram below, two circles intersect at K and Y. The larger circle passes through O, the centre of the smaller circle. T is a point on the smaller circle such that KT is a tangent to the larger circle. TY produced meets the larger circle at W. WO produced meets KT at E.

Let  $\hat{W}_1 = x$



- 12.1 Determine FOUR other angles, each equal to  $x$ . (8)
  - 12.2 Prove that  $\hat{T} = 90^\circ - x$ . (3)
  - 12.3 Prove that  $KE = ET$ . (3)
  - 12.4 Prove that  $KE^2 = OE \cdot WE$ . (6)
- [20]**