



# basic education

Department:  
Basic Education  
**REPUBLIC OF SOUTH AFRICA**

## SENIOR CERTIFICATE/ NATIONAL SENIOR CERTIFICATE

**KEREITI 12**

**DIPALO P2**

**LOETSE 2021(2)**

**MATSHWAO: 150**

**NAKO: Dihora tse 3**

**Pampiri ena ena le maqephe a 15 le leqephe le 1 la tlhahisoleseding.**



**DITAELO LE TLHAHISOLESEDING**

Bala ditaelo tse latelang ka hloko.

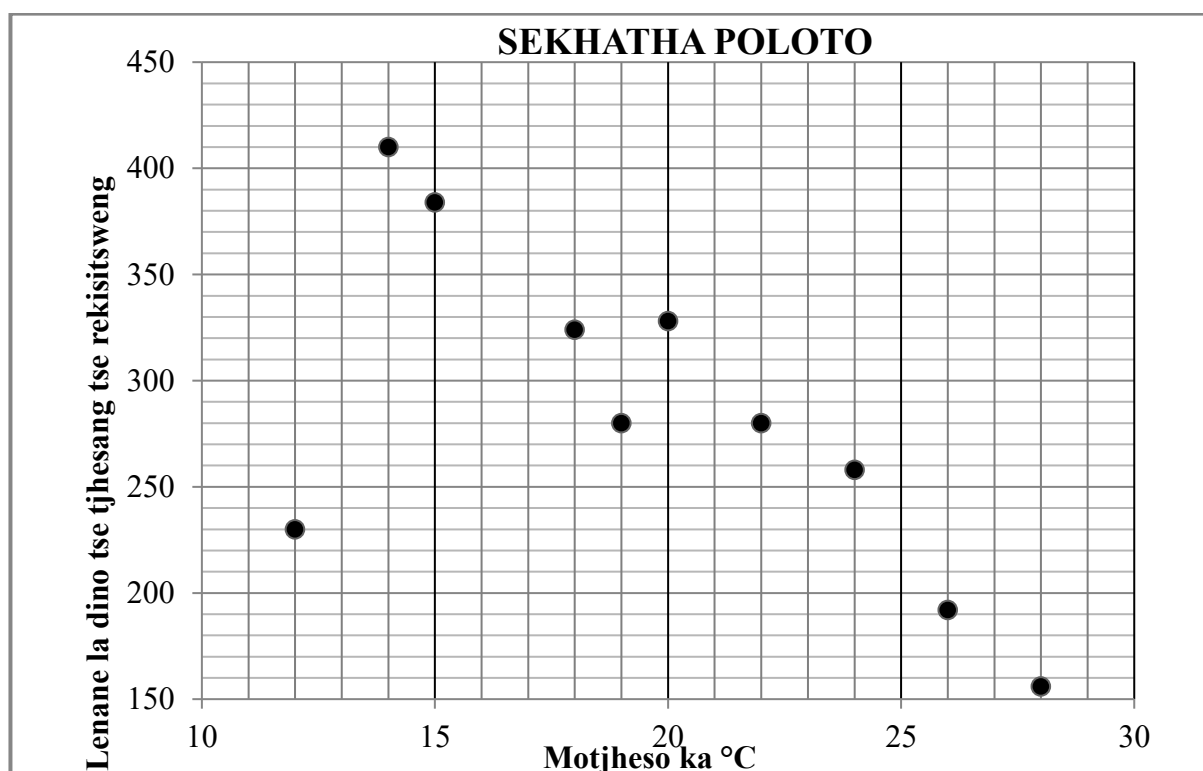
1. Ena pampiri ena le dipotso tse 10.
2. Araba dipotso TSOHLE ho BUKANA E IKGETHILENG YA HO ARABELA.
3. Ka makgethe BONTSHA tsohle dipalo, ditshwantsho, dikerafo, jwalojwalo. tseo o di sebedisitseng ho fumana dikarabo tsa hao.
4. Dikarabo feela di KEKE tsa fumana matshwao kaofela ka nako tsohle.
5. Oka sebedisa khalukhetara e dumelletsweng ya saense (esa porogeremuang ebile ena le dikerafo), kante le haeba ho boletswe ka tsela e nngwe.
6. Moo ho hlokahalang teng, atametsa dikarabo tsa hao ho desimale tse PEDI, kante le haeba ho boletswe ka tsela e nngwe.
7. HAHO bolele hore ditshwantsho tsohle di takuwe ho latela ditekanyo tse nepahetseng.
8. Leqephe la tlhahisoleding le nang le di-fomula le teng moo pampiri e fellang teng.
9. Ngola ka makgethe leka tsela e bonahalang.



**POTSO 1**

Mokete wa selemo wa dipapadi o tshwerwe nako ya matsatsi a 11. Lebenkele le rekisa dino tse tjhesang moketeng ona. Ho letsatsi le leng le leng ho matsatsi a pele a 10, monga lebenkele o ile a ngola mofuthu ka 13:00 le palo ya dino tse tjhesang tse rekisitsweng. Tlhalisoleseding ena e bontshitswe tafoleng leho sekhatha poloto ka tlase.

<b>Mofuthu (in °C)</b>	14	24	26	18	20	28	22	15	12	19
<b>Palo ya dino tse tjhesang tse rekisitsweng</b>	410	258	192	324	328	156	280	384	230	280



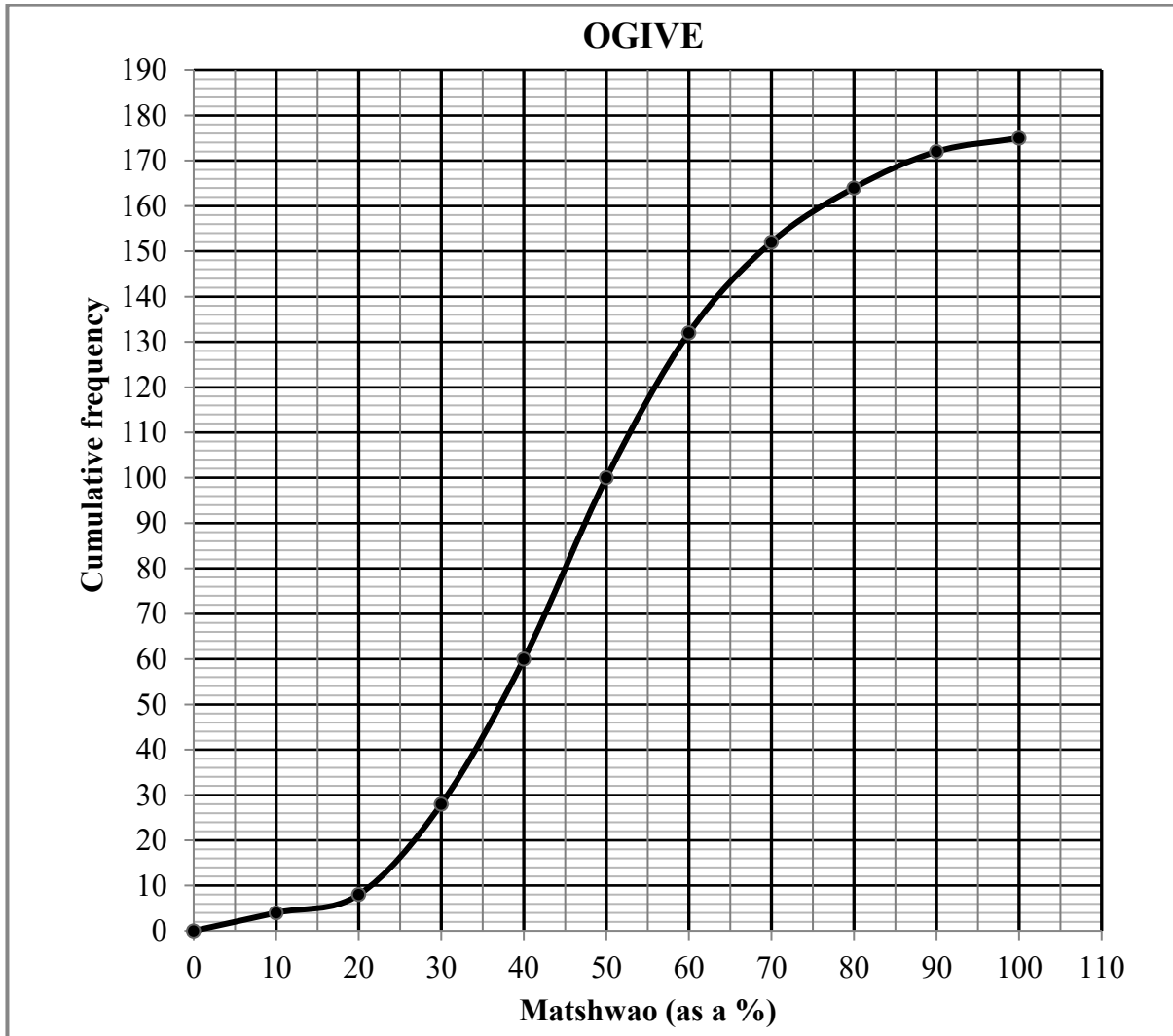
- 1.1 Hlalosa mkgwa oo data eo bontshang. (1)
- 1.2 Fumana ekweshini ya mola wa disekwere tse nyane tsa rekereshene tsa datha. (3)
- 1.3 Monga lebenkele o hlokometse hore o sebedisitse litara ele nngwe ya lebeso ho dikopi tse 8 tsa dino tse tjhesang tse rekisitsweng. Haeba mofuthu ka 13:00 ka letsatsi labo 11 ene lebelletswe hoba 17 °C, akanya lenane la lebokoso la litara ele nngwe ya lebeso monga lebenkele a tlamehang ho e reka ka letsatsi la bo 11. (3)
- 1.4 Kgetha outlier ho datha. (1)

[8]



**POTSO2**

2.1 Baithuti hotswa dikolong tse fapaneng ba ngotse teko tsa mahlale hore ba kgone hore ba khwalifaye ho fumana basari. Matshwao a bona (ka peresente) a bontshitswe ho ogive (cumulative frequency kerafo) ka fatshe.



- 2.1.1 Ho ngotse baithuti ba bakae teko? (1)
- 2.1.2 Ngola modal class ya data. (1)
- 2.1.3 Matshwao a tlase a ho khwalifayela basari ke 75%. Ke ba bake baithuti batla khwalifayela basari? (2)



2.2 Tafole e latelang e bontsha matshwao a baithuti ba 15 hotswa sekolong se itseng a fumanweng ho teko ya mahlale.

<b>Matshwao (ka%)</b>	62	58	78	85	74	48	74	84	100	46	80	92	60	90	92
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Fumana:

2.2.1 Letshwao la mini le fumanweng ke baithuti. (2)

2.2.2 Setandade devieshene ya matshwao a baithuti. (1)

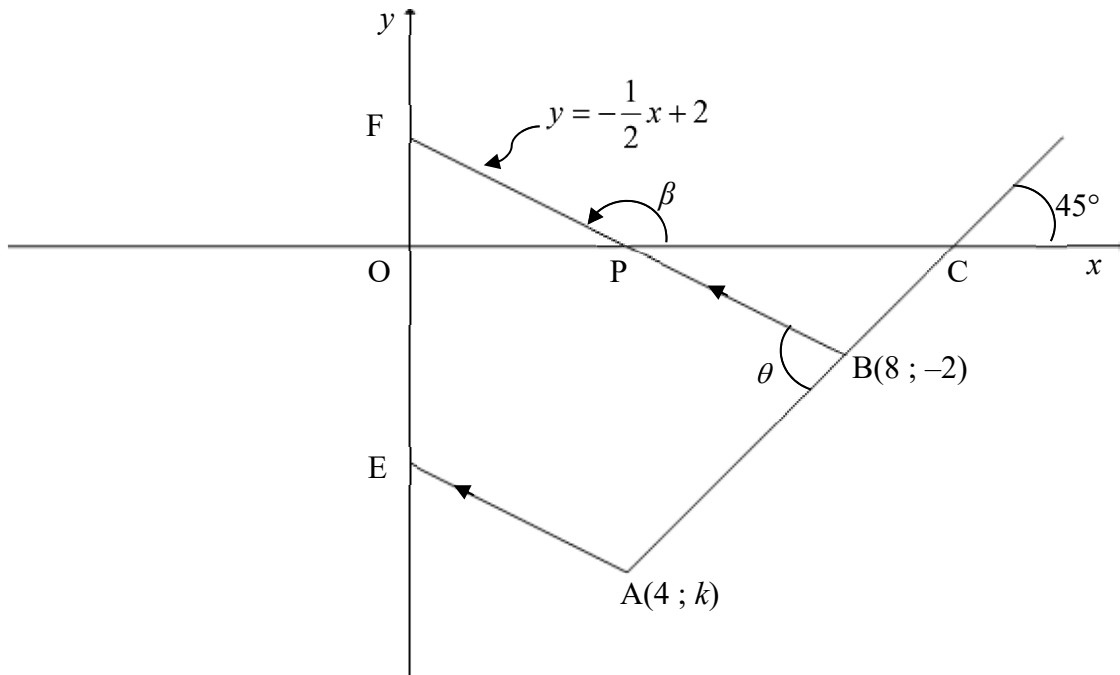
2.2.3 Lenane la baithuti bao matshwao a bona a fumanhang ho feta setandathe devieshene sele seng ka hodimo ho mini. (2)

2.3 Matshwao a Kereiti 11 (ka persente) aho qetela a fumanweng ke baithuti a lekotswe. Setandathe devieshene sele seng ho inthavale ya mini e fumanwe ele (82,7; 94,1).

Fumana setandathe devieshene ya matshwao aho qetela a Kereiti 11. (3)  
**[12]**

**POTSO 3**

Ho setshwantsho se latelang, mola wa BF o takilwe hotswa ho B(8 ; -2) ho kgaola  $x$ -axis ho P le  $y$ -axis ho F. Engele ya inclination BF ke  $\beta$  le ekweshene ya BF  $y = -\frac{1}{2}x + 2$ . Hotswa ho A(4 ; k), mola o mong o takilwe o pharalele ho BF le ho kgaola  $y$ -axis ho E. Mola o fetang ho A le ho B ena le inclination ya  $45^\circ$  le ho kgaola  $x$ -axis ho C.  $\hat{A}BF = \theta$ .



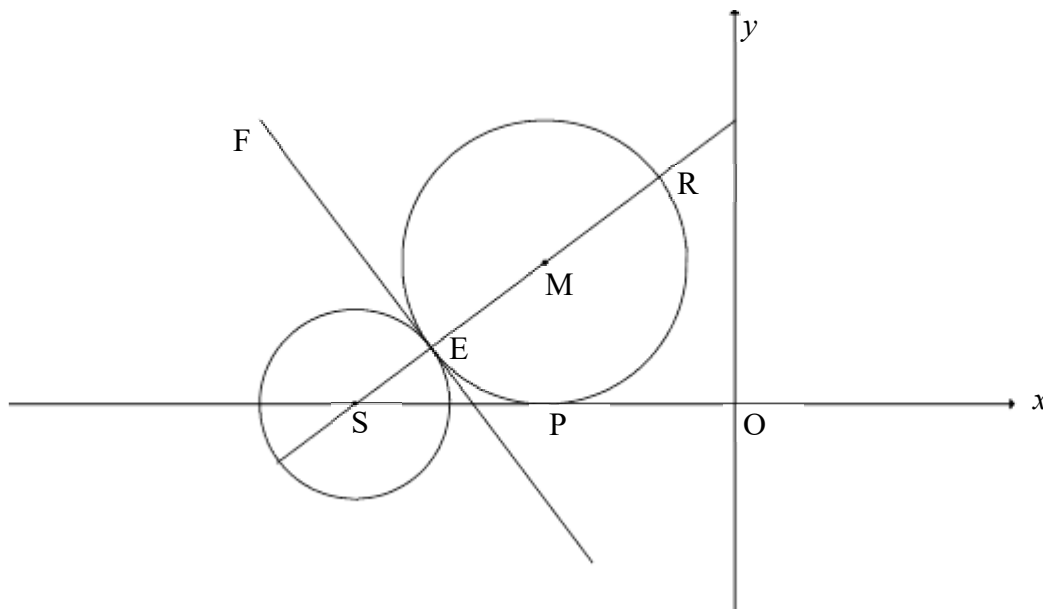
- 3.1 Batla keradiante ya AB. (1)
- 3.2 Bontsha hore velu ya  $k$  ke  $-6$ . (2)
- 3.3 Fumana ekweshini ya EA ka tsela ya  $y = mx + c$ . (3)
- 3.4 Fumana:
  - 3.4.1 Boholo ba  $\theta$  (3)
  - 3.4.2 Bolelele ba BF (3)
  - 3.4.3 Eria ya  $\triangle ABF$  (4)
- 3.5 Haeba G ke ntlha e khwaderanteng ya bone hore APBG ebe pharalelokereme. Fumana boholo ba  $\hat{P}AG$ . (4)

**[20]**



**POTSO 4**

Ho setshwantsho se latelang, S ke ntlha ho  $x$ -axis. Sedikadikwe se nang le bohare S le sedikadikwe se nang le bohare M di takilwe. Didikadikwe tse pedi di kopana kante ho E. FE ke thanjente ya didikadikwe tse pedi ho E. Sedikadikwe sa bohare ba M, ena le ER ele diametha, e kopana le  $x$ -axis ho P.

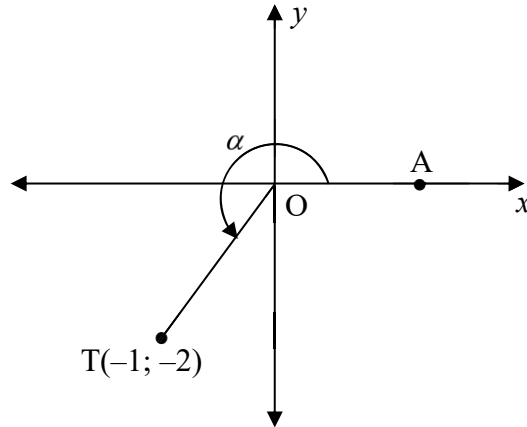


- 4.1 Ekweshini ya sedikadikwe se nang le bohare S ke  $(x+8)^2 + y^2 = 4$ .
- 4.1.1 Fumana dikhoodinetse tsa S. (2)
- 4.1.2 Bontsha hore diametha ya sedikadikwe sa bohare ba S ke diyuniti tse 4. (1)
- 4.2 Haeba re boela re nehwa hore  $SR = 8$  diyuniti le  $R\left(-\frac{8}{5}; \frac{24}{5}\right)$ , bala::
- 4.2.1 Bolelele ba EM (2)
- 4.2.2 Keradiante ya thanjente FE (3)
- 4.2.3 Khoodinetse tsa M (4)
- 4.2.4 Khoodinetse tsa E (2)
- 4.3 Sedikadikwe sa bohare ba  $M(-4; 3)$  e shifotile uniti e 1 hoya ka letsohong le leqele le ho refolekotiwa ho  $x$ -axis ho fumana sedikadikwe se setjha ho K. Fumana hore ntlha  $(-8; 0)$  eka hare kapa kante ho sedikadikwe ho K. Bontsha mesebetsi YOHLE. (5)

**[19]**

**POTSO 5**

- 5.1 Ntlha  $T(-1; -2)$  re e nehilwe setshwantshong se ka fatshe. A ke ntlha ho  $x$ -axis hore reflex  $\widehat{A\hat{O}T} = \alpha$ .



Fumana, **ntle le tshebediso ya khalukhetara**, velu ya tse latelang:

5.1.1  $\tan \alpha$  (1)

5.1.2  $\cos \alpha$  (2)

5.1.3  $\cos(\alpha + 45^\circ)$  ho foromo e bobebe. (4)

- 5.2 Fumana, **ntle le tshebediso ya khalukhetara**, velu ya expression tse latelang:

$2\sin(-20^\circ) \cdot \sin 160^\circ - \cos 40^\circ$  (4)

- 5.3 Ela hloko:  $3 \cos x \cdot \sin x + \tan x \cdot \cos^2(180^\circ - x)$

5.3.1 Etsa expression ena ebe bobebe hoya ho trigonometric reshio ele nngwe. (4)

- 5.3.2 Ebe, o ngola renje ya:

$f(x) = 3 \cos x \cdot \sin x + \tan x \cdot \cos^2(180^\circ - x)$  (2)

5.4 Pruva identity:  $\frac{\cos 3x}{\cos x} = 4 \cos^2 x - 3$  (5)

- 5.5 Fumana jeneral solushene ya  $x$  ho ekweshini e latelang:

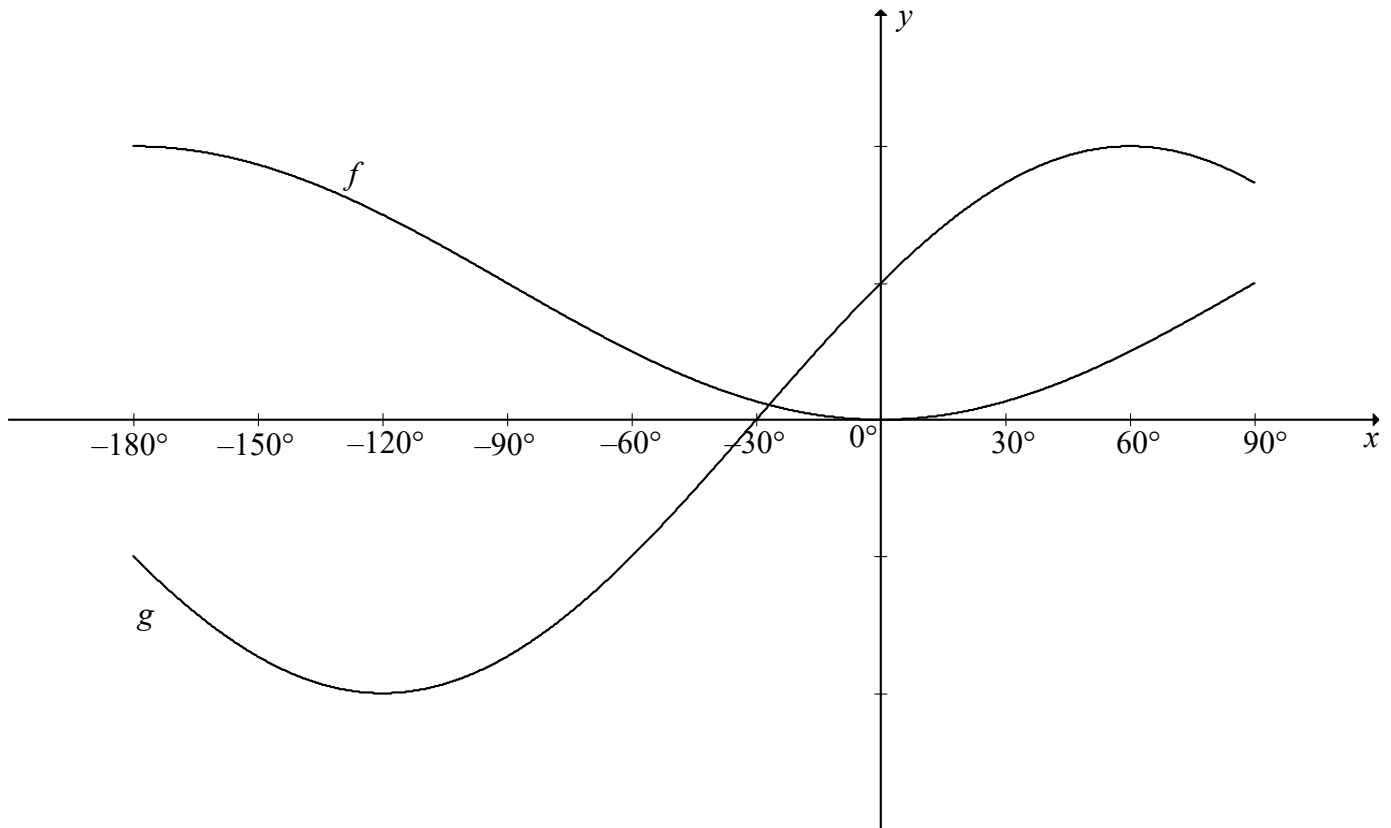
$3^{2 \tan x} - 3^{\tan x + 1} = 54$  (5)

[27]



**POTSO 6**

Setshwantshong se latelang, kerafo ya  $f(x) = -\cos x + 1$  le  $g(x) = 2\sin(x + 30^\circ)$  di takilwe ho inthavale  $x \in [-180^\circ; 90^\circ]$ .



6.1 Ke velu efe ya  $x$ ,  $x \in [-180^\circ; 90^\circ]$ , moo:

6.1.1  $f(x) \cdot g(x) \geq 0$  (2)

6.1.2  $g(x) = -1$  (2)

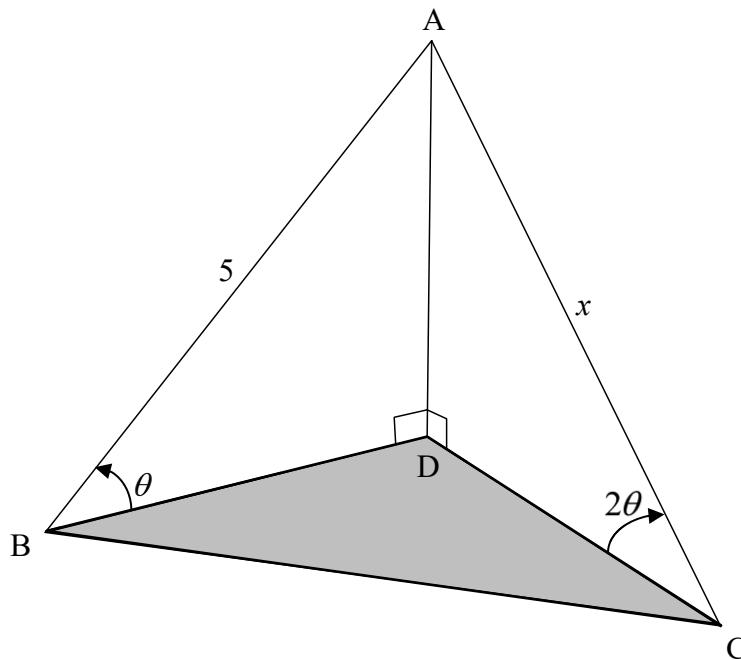
6.2  $y$ -axis e tsamaisitswe  $90^\circ$  hoya ka letsohong le letona. Fumana ekweshini e ntjha ya kerafo eo qalong e ile ya bitswa  $f$ , ho foromo e bobebe.

(2)  
[6]



**POTSO 7**

Setshwantshong se latelang, B, C and D di sebakeng se tshwanang se tshekaletseng. AD ke palo e tsepameng e tsheheditsweng ke dithapo tse pedi, AB and AC. Engele tsa eleveishene ho qala ho B le C hoya ho A, tsullung ya palo, ke  $\theta$  le  $2\theta$  ka ho latellana.  $AB = 5$  diyuniti le  $AC = x$  diyuniti.

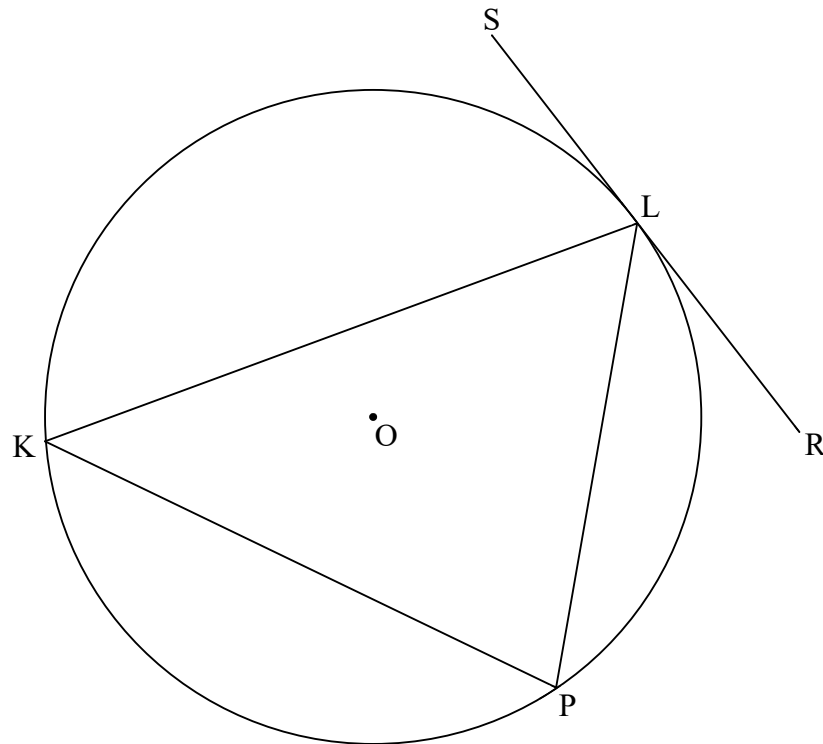


7.1 Bontsha hore  $x = \frac{5}{2 \cos \theta}$  (5)

7.2 Bala bolelele ba BC haeba re nehilwe hore  $\hat{BAC} = 112^\circ$  le  $\theta = 30^\circ$ . (3)  
[8]

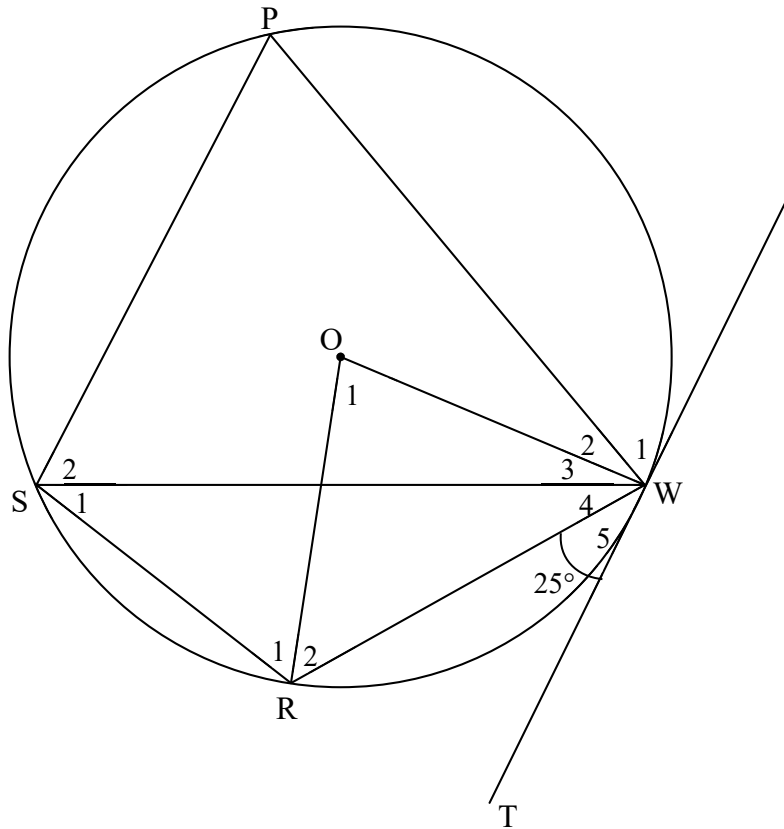
**POTSO 8**

- 8.1 Setshwantshong se latelang, dikhodo KL, LP and KP di takilwe ka hare ho sedikadikwe, se nang le bohare ba O. SLR ke thanjente ya sedikadikwe ho L.



Pruva theoreme e bolelang hore engele pakeng tsa thanjente SLR le khodo KL e lekana le engele e fumanehang ho althanete segmente, ka hoo pruva hore  $\hat{SLK} = \hat{P}$ . (6)

8.2 Ho setshwantsho se latelang,  $PWRS$  ke saetliliki khwaderilatherale ka hare ho sedikadikwe, bohareng ho  $O$ .  $\triangle PSW$  ke ekhwilaterale teraengele.  $TW$  ke thanjente ya sedikadikwe ho  $W$ . Radii  $OR$  le  $OW$  di takilwe.  $\hat{W}_5 = 25^\circ$ .



8.2.1 Fumana, o fana ka mabaka, boholo ba:

(a)  $\hat{S}_1$  (2)

(b)  $\hat{O}_1$  (2)

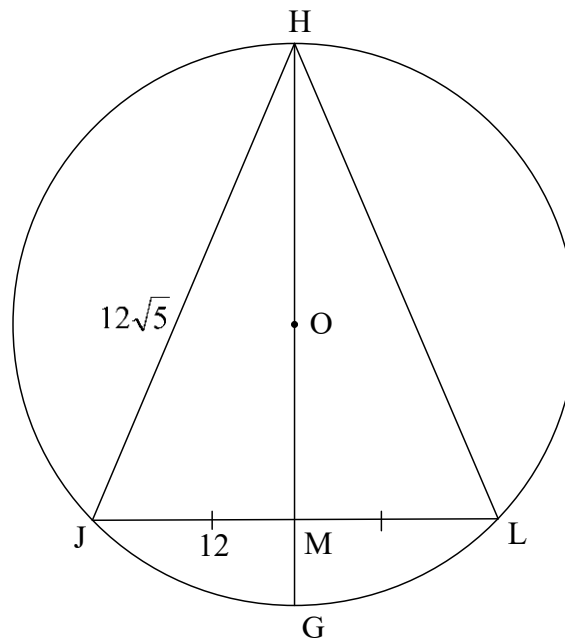
(c)  $\hat{R}_1$  (5)

8.2.2 Pruva hore  $SP \parallel TW$ . (3)



8.3 Setshwantshong se latelang, sedikadikwe se nang le bohare O se takilwe. H, J, G and L ke dintlha tse hodima sedikadikwe.  $\triangle HJL$  e takilwe. HOG e kgaola JL mahareng ho M.

$HJ = 12\sqrt{5}$  diyuniti and  $JM = 12$  diyuniti.

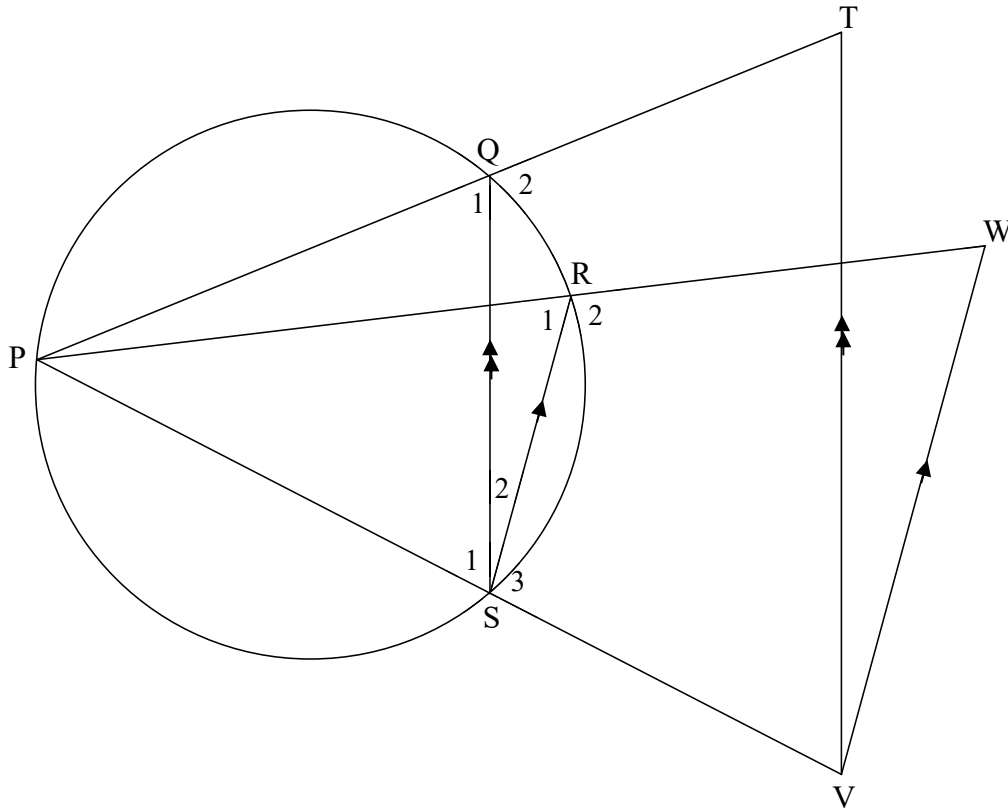


8.3.1 Haeba  $MG = 6$  diyuniti le  $OM = x$ , ngola HM ka mokgwa wa  $x$ . (2)

8.3.2 Bala, o fana ka mabaka, bolelele ba radiase ya sedikadikwe. (5)  
[25]

**POTSO 9**

Setshwantshong se latelang, P, Q, R and S ke dintlha tse hodima sedikadikwe. PS, PQ le PR di lelefaditswe hoja ho V, T le W ka ho latelanang. VT || SQ le SR || VW.



Pruva, o fana ka mabaka, hore:

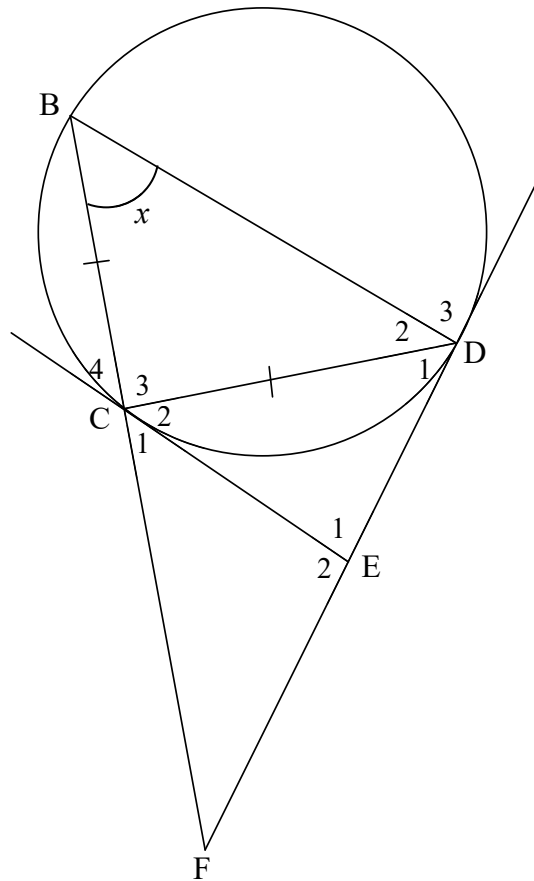
9.1  $\frac{TQ}{QP} = \frac{WR}{RP}$  (3)

9.2 TPVW ke setliliki khwadilatherale (5)  
[8]



**POTSO 10**

Setshwantshong se latelang, B, C le D ke dintlha tse hodima sedikadikwe hore  $BC = CD$ . EC le ED ke di thanjente hodima sedikadikwe ho C le D ka ho latellana. BC e lelefaditswe ho kopana le thanjente ho DE e lelefaditsweng hoyo ho F.  $\hat{B} = x$ .



10.1 Pruva, o neha mabaka, hore:

10.1.1  $\hat{E}_1 = 180^\circ - 2x$  (5)

10.1.2  $\triangle ECD \parallel\parallel \triangle CBD$  (3)

10.2 Pruva, o fan aka mabaka, hore:

10.2.1  $CD^2 = CE \cdot BD$  (3)

10.2.2  $\frac{CF^2}{EF^2} = \frac{BD}{DE}$  (6)

[17]

**KAOFELA: 150**

a



## LEQEPHE LA TLHAHISOLESING

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1 + ni)$$

$$A = P(1 - ni)$$

$$A = P(1 - i)^n$$

$$A = P(1 + i)^n$$

$$T_n = a + (n - 1)d$$

$$S_n = \frac{n}{2}[2a + (n - 1)d]$$

$$T_n = ar^{n-1}$$

$$S_n = \frac{a(r^n - 1)}{r - 1}; r \neq 1$$

$$S_\infty = \frac{a}{1 - r}; -1 < r < 1$$

$$F = \frac{x[(1 + i)^n - 1]}{i}$$

$$P = \frac{x[1 - (1 + i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x + h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$M\left(\frac{x_1 + x_2}{2}; \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c$$

$$y - y_1 = m(x - x_1)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \tan \theta$$

$$(x - a)^2 + (y - b)^2 = r^2$$

$$\text{In } \Delta ABC: \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cdot \cos A$$

$$\text{area } \Delta ABC = \frac{1}{2} ab \cdot \sin C$$

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

$$\cos 2\alpha = \begin{cases} \cos^2 \alpha - \sin^2 \alpha \\ 1 - 2\sin^2 \alpha \\ 2\cos^2 \alpha - 1 \end{cases}$$

$$\sin 2\alpha = 2\sin \alpha \cos \alpha$$

$$\bar{x} = \frac{\sum x}{n}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

$$P(A) = \frac{n(A)}{n(S)}$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\hat{y} = a + bx$$

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$

