



# MATHEMATICS GRADE 9



# DATE: ..... TOPIC: Functions and Relationships

### CONCEPTS & SKILLS TO BE ACHIEVED: By the end of the lesson learners should know and be able to:

- Determine input values, output values or rules for patterns and relationships using, tables, formulae, equations
- Determine, interpret and justify equivalence of different descriptions of the same relationship or rule presented:
  - by equations/expressions
  - by graphs on a Cartesian plane

RESOURCES:	DBE Workbook, Sasol-Inzalo book, Textbooks,
	Refer to page 12 and 15. When you see the icon below:
ONLINE RESOURCES	WATCH NOW







# DAY 1: LESSON DEVELOPMENT

Introduction - Let's consider the following 4 situations:

There are two quantities in each situation (Pay attention to how these quantities behave.)

1. The number of calls you make, and the airtime left on your cell phone.

**4** The more calls you make, the less airtime will be left on your cellphone.

2. The number of learners at a school and the number of classrooms needed.

**4** The more learners, the more classrooms needed.

3. The number of songs performed and the duration of the concert.

**4** The more songs performed , the longer the concert.

4. The number of matches in each arrangement, and the number of triangles in the arrangement:



**4** As more triangles are made, more matches are needed.

### What do we notice:

The one variable quantity is influenced by another, we say there is a **<u>relationship</u>** between the two variable quantities.

Let's take it a step further:

A relationship between two variables in which there is only one output number for each input number, is called a **<u>function</u>**.







# Let's illustrate:

The price the customer pays is dependent on how many cans of coke he buys.

A can of Coke costs R10.

If you put two R10 notes in the Coke Machine, determine how many can(s) you will receive.







# CLASSWORK:

Machine diagrams are used to represent functions. In the function machine below, the inputs are labelled  $\mathbf{x}$  of the function and the outputs are labeled  $\mathbf{y}$  of the function.





# CONSOLIDATION

# IT IS IMPORTANT TO REMEMBER:

## **Relation**:

If one variable quantity (input value) is influenced by another (output value), we say there is a **relationship** between the two variables.

### Function:

A function is an equation/rule which shows the relationship between the input and the output and where there is exactly one output for each input.

## Output value:

Value that you obtain when you apply the rule to the input numbers.

## Input value:

The input is the number you feed into the function rule.

# HOMEWORK:

Create your own rule in the function machine. Write your rule in the white box of the machine. Set an input value and calculate the output value.









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1. For each output, multiply the input by 4, then subtract 5.

Input x	2	3	4	7	a	b
Output y	3	7	11	23	35	55

2. 
$$y = \frac{x}{2} + 4$$

Input x	с	2	4	10	d	е
Output y	4	5	6	9	12	17

3. Find the missing values of **p**, **q**, **r**, **s** and **t**.



# CONSOLIDATION

# IT IS IMPORTANT TO NOTE:

Alternative method:

If the output value (y) is given, it can be substituted in the formula and solving this equation gives an input value (x).

Example: Input value(x)  $\implies y = 2x - 3 \implies 13$ 

Output value 13 is given, it can be substituted in the formula to produce the equation and solving this equation using inverse operation gives an input value of x = 8.







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**Functions and Relationships** 





A set of rectangles all have a perimeter of 24 units. The breadth of each rectangle (y) varies in relation to the length (x) using the **formula** 2(x + y) = 24. Complete the table of values to represent this situation.

x	1	2	3	4	6					
у						5	4	3	2	1

		DAY	3:		
	l	ESSON DEVE	LOPMENT		
Finding the Fund	ction Rule:				ł <mark></mark>
Example 1					**
Rule: y =?					<b>E</b>
Input 1 Output 3	2 5 +2 +2	3 7 +2	4		
The input values i The common diff	ncrease by 1 eac erence between	ch time and the o the output value	putput values incre es is 2.	ease by 2 each tin	ne.
This tells us that th the function is 2 ×	the first operation $x$	performed on the	e input was to mult	iply it by 2. Hence	e, part of
$y = 2 \times x$					
We now must de	termine the relation	onship between	the input values a	nd output values.	
Input (r)	15	2	3	4	
$2 \times x$	2 x 1 +	2 x <b>2</b> +	_ 2x3+	2 x 4 +	
Output (y)	3	5	7 🗸	9	
Input (x)	1	2	3	4	
$2 \times x$	2 x 1 + 1	2 x <b>2</b> + 1	2 x <b>3 +</b> 1	2 x <b>4</b> + 1	
Output (y)	3	5 <	/ •	9 🥒	
Hence, our rule is	2x + 1 which, as	a function relatir $\therefore y = 2x$	$\begin{array}{ll} \text{ng } x \text{ and } y, \text{ is } y = \\ +1. \end{array}$	$2 \times x + 1$ .	
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**Functions and Relationships** 

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Example 2

Find the function rule for the following input-output table.







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# CLASSWORK:

Find the rules for the following function tables.

1	

x	1	2	3	4	5
у	10	14	18	22	26

2.

x	1	4	10
у	9	12	18

3. Find the function rule for this table. Then calculate the two missing numbers.

x	12	13	14	15	16
у	76	82	88	a	b

# HOMEWORK:

At Sunningdale Primary School, seventh graders spend 3 hours every night studying, eighth graders spend 4 hours, nine graders spend 5 hours.

Let the students' grade be the input (x). What is the function rule between the students' grade and the amount of time the students spend on homework every night?







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## Representation of a Function

Discuss:

A functional rule can be **represented** in a variety of ways.

For example, we can indicate how to get from a **function's** input to its output using a **formula**, a **graph**, or a **table** of values and a **flow diagram**.























# **HOMEWORK:**



# Section A

On separate pages, represent each of the following functions with the following:

- (a) a flow diagram
- (b) a table of values for the set of integers from -5 to 5
- (c) a graph

1. The relationship described by the expression 3x + 4.

2. The relationship described by the expression -3x + 4.

3. The relationship described by the expression  $\frac{1}{2}x + 2$ .

## Section B

Match each of the four equations provided below with one of the following tables of the values and a graph.

1.1 y = 2x + 4 $1.2 \ 2x + 3y = 6$ 

1.3 xv = 12

1.6 
$$xy = 12$$
  
1.4  $y = x^2 - 1$ 

У

Table A	Х	-3	0	2	9	11	20
	У	8	-1	3	80	120	399
Table B							
	х	1	2	3	4	6	12
	у	12	6	4	3	2	1
Table C							
	х	-3	0	3	6	9	12
	У	4	2	0	-2	-4	-6
Table D							
	Х	2	4	5	8	15	50
	У	8	12	14	20	34	104



![](_page_13_Picture_19.jpeg)

![](_page_13_Picture_21.jpeg)

![](_page_14_Picture_0.jpeg)

![](_page_14_Picture_1.jpeg)

# DAY 5: REVISION

Let's revise what we have learned this week:

• A function is a relationship between an input and an output which assigns exactly one output to each input.

![](_page_14_Picture_5.jpeg)

![](_page_14_Picture_6.jpeg)

- A **function rule** is an equation that describes the relationship between inputs and outputs.
- The input of a function is the number you feed into the expression.
- **The output** of a function is the value that results from substituting in a value for the input.

Let's illustrate:

![](_page_14_Figure_11.jpeg)

Lastly, let's remember, a functional rule can be represented in a variety of ways.

# Let's illustrate:

Graph the function rule y = x - 1, using the inputs -1, 0, 1, 2:

Input, <i>x</i>	<i>x</i> – 1	Output, y	Ordered Pair, (x, y) ▼			3-2-	y			/
-1	-1 - 1	-2	(-1, -2)	<b>*</b> (C	), -	1)-	(2,	1)		
0	0 - 1	-1	(0, -1)	<b>≺</b> −3 −2	2 - 1	Ż		2	2 3	$x \rightarrow x$
1	1 - 1	0	( <mark>1, 0</mark> )	(-1, -	-2)		[	(1,	0)	
2	2 - 1	1	(2, 1)			-3-	r			

![](_page_14_Picture_16.jpeg)

![](_page_15_Picture_0.jpeg)

![](_page_15_Picture_1.jpeg)

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# **CLASSWORK:**

1. Copy and complete the following table for the relationship described by  $y = x^2$ .

x	-5	-4	-3	-2	-1	0	1	2	3	4	5
у											

On a graph sheet, copy the axis as below and represent the ordered number pairs in the table and join the points.

![](_page_15_Figure_6.jpeg)

2. Copy and complete the table for the relationship y = 15 + x. Represent the ordered number pairs on the graph sheet and join the points.

x	-15	-10	-5	0	5	10	15
у							

![](_page_15_Figure_9.jpeg)

![](_page_15_Picture_10.jpeg)

![](_page_16_Picture_0.jpeg)

![](_page_16_Picture_1.jpeg)

cation

![](_page_16_Picture_2.jpeg)

3. Copy and complete the table for the relationship y = 15 - x. Represent the ordered number pairs on the graph sheet and join the points.

![](_page_16_Figure_4.jpeg)

![](_page_16_Picture_5.jpeg)

![](_page_17_Picture_0.jpeg)

![](_page_17_Picture_1.jpeg)

## MEMORANDUM: DAY 1:

Classwork:

y = 2x + 51.1 y = 2(7) + 5 y = 14 + 5 y = 191.2 y = 2(-2) + 5 y = -4 + 5 y = 11.3 y = 2(1) + 5 y = 2 + 5y = 7

2.1  $y = x^2 + 2x + 3$ 

Input values: x	-1	0	1	2
Output values: y	2	3	6	11

### Homework:

Any mathematically sound answer is accepted.

## MEMORANDUM: DAY 2:

Example:

![](_page_17_Figure_11.jpeg)

![](_page_17_Picture_12.jpeg)

![](_page_18_Picture_0.jpeg)

![](_page_18_Picture_2.jpeg)

# **Classwork:**

1.

<b>10</b> $\leftarrow$ divide by 4 $\leftarrow$ add 5 $\leftarrow$ 35	∴ a = 10
<b>15</b> $\leftarrow$ divide by 4 $\leftarrow$ add 5 $\leftarrow$ 55	∴ b = 15
2.	
$0 \leftarrow \text{multiply by } 2 \leftarrow \text{subtract } 4 \leftarrow 4$	∴ c = 0
<b>16</b> $\leftarrow$ multiply by 2 $\leftarrow$ subtract 4 $\leftarrow$ 12	∴ d = 16
<b>26</b> $\leftarrow$ multiply by 2 $\leftarrow$ subtract 4 $\leftarrow$ 17	∴ e = 26
3.	
$p \rightarrow x^2 - 10 \rightarrow 15$	
$\pm 5 \leftarrow \text{square root} (\sqrt[2]{)} \leftarrow \text{add } 10 \leftarrow 15$	∴p=±5
$q \rightarrow x^2 - 10 \rightarrow 39$	
$\pm 7 \leftarrow \text{square root} (\sqrt[2]{}) \leftarrow \text{add } 10 \leftarrow 39$	∴ q = <u>+</u> 7

# OR

$p^{2} - 10 = 15$ $\sqrt[2]{p^{2}} = 25$ $p = \pm 5$	$q^{2} - 10 = 39$ $\sqrt[2]{q^{2}} = 49$ $q = \pm 7$	
$r = (-3)^2 - 10$	$s = (-1)^2 - 10$	$t = (3)^2 - 10$
r = 9 - 10	s = 1 - 10	t = 9 - 10
r = -1	s = -9	t = -1

Homework: 
$$2(x + y) = 24$$
.

x	1	2	3	4	6	7	8	9	10	11
у	11	10	9	8	6	5	4	3	2	1

2(x + y) = 24

so, x + y = 12.

When y = 5, x = 7.

![](_page_18_Picture_12.jpeg)

![](_page_19_Picture_0.jpeg)

![](_page_19_Picture_1.jpeg)

## **MEMORANDUM: DAY 3:**

### **Classwork:**

1. y = 4x + 62. y = x + 83. y = 6x + 4 a = 94; b = 100

### Homework:

![](_page_19_Figure_6.jpeg)

Students Grade x	7		8		9	
$1 \times x$		$1 \times 7 - 4$		1×8-4		1×9-4
Time spent in hours $y$	3 🗸		4 🧹		5 🧹	

 $\therefore y = x - 4$ 

![](_page_19_Picture_9.jpeg)

![](_page_20_Picture_0.jpeg)

**MEMORANDUM: DAY 4:** Classwork: (starter activity)

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Y F U G Q н J В 5 0 Т V Ρ Α Μ 2 Ζ 8 Ъ-<mark>8</mark> -7x -6 Ps . Ν З С 4 -5 L Е -6 Υ 8 Κ 9 Tell what point is located at each ordered pair. 1) (-9,-1) <u>D</u> 3) (-3,+5) <u>J</u> 5) (-6,+2) <u>V</u> 7) (+7,-6) <u>E</u> 2) (+4,+7) **Q** 4) (+7,+3) **T** 6) (-2,+8) **F** 8) (-2,-3) **N** Write the ordered pair for each given point. 11) **H** (-7,+5) 13) **Z** (-2,+0) 15) **P** (+1,+2)M (+9,+2) 9) **G** (-3,+7) 12) **O** (-7,+3) 14) **I** (-8,-6) 16) **A** (+7,+2)10) Plot the following points on the coordinate grid. 17) **S** (-3,-1) 19) **U** (-4,+7) 21) **X** (-7,-1) 23) **Y** (+7,-7) 22) **K** (+3,-9) 18) L (-4,-6) 20) **B** (+2,+5) 24) **C** (-5,-4) Functional Schools Grade 9 **Functions and Relationships** 

![](_page_21_Picture_0.jpeg)

![](_page_21_Picture_1.jpeg)

## Homework:

<u>Section A</u>

![](_page_21_Figure_4.jpeg)

2.

![](_page_21_Figure_6.jpeg)

![](_page_21_Picture_9.jpeg)

![](_page_22_Picture_0.jpeg)

![](_page_22_Picture_1.jpeg)

3. 0 -5 -4 0 2 3 4 5 x -3 2 -1 1  $3\frac{1}{2}$  $\frac{1}{2}x + 2$ 0 1 11 2  $2\frac{1}{2}$ 3 4  $4\frac{1}{2}$  $y = \frac{1}{2}x + 2$ 6 5 4 3 1 2 -3 4 Section **B** 1.1  $y = 2x + 4 \rightarrow \text{Table D} \rightarrow \text{Graph B}$ (2;8): y = 2x + 4  $\therefore y = 2(2) + 4$   $\therefore y = 8$ (0; 4): y = 2x + 4  $\therefore y = 2(0) + 4$   $\therefore y = 4$ 1.2  $2x + 3y = 6 \rightarrow \text{Table C} \rightarrow \text{Graph C}$ 1.3  $xy = 12 \rightarrow \text{Table B} \rightarrow \text{Graph D}$  $\begin{array}{rcl} (6;2)\colon xy \ = \ 12 & \ddots & (6)(2) \ = \ 12 \\ (1;12)\colon & \ddots & (1)(12) \ = \ 12 \end{array}$ 1.4  $y = x^2 - 1 \rightarrow \text{Table A} \rightarrow \text{Graph A}$  $(0; -1): y = (0)^2 - 1 \quad \therefore \quad y = -1$  $(-3;8): y = (-3)^2 - 1 \quad \therefore \quad y = 9 - 1 \quad \therefore \quad y = 8$ 

![](_page_22_Picture_3.jpeg)

![](_page_23_Picture_0.jpeg)

![](_page_23_Picture_1.jpeg)

## **MEMORANDUM: DAY 5:**

#### **Classwork:**

![](_page_23_Figure_4.jpeg)

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![](_page_24_Figure_0.jpeg)

![](_page_24_Picture_1.jpeg)

![](_page_25_Picture_0.jpeg)

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GRADE: 9

**ASSESSMENT / REVISION TASK** 

## TOPIC: FUNCTIONS & RELATIONSHIPS

### <u>Question 1</u>

In a discussion between Madison and Benjamin about functions, Benjamin said that the diagram below represents a function, but Madison argued that it does not. Who is right?

Motivate your answer.

![](_page_25_Figure_7.jpeg)

### Question 2

Complete the following flow diagrams:

![](_page_25_Figure_10.jpeg)

2.3 In each case consider the input values and state whether they are irrational numbers, natural or rational numbers.

![](_page_25_Picture_12.jpeg)

![](_page_26_Picture_0.jpeg)

![](_page_26_Picture_1.jpeg)

# Question 3

ſ	`⊥ + ?>€		1 +1 V	+5 27		$\rightarrow$ +1 $\gg$	0 +1 Sr C	.0 Sr
6	7	8	9	10	15	20	30	40
		22	25	28	43	58	88	
L +	シ く +	ے بر +	D € +	♪~ +	シ く +	シ へ +	≥ ¢ +	Ŀ,
	6		$\begin{array}{c ccccccccccccccccccccccccccccccccccc$					

- 3.1 Copy and complete the table.
- 3.2 By how much will the output number increases if the input number increases by 1?
- 3.3 Determine the function rule for the function table above.

![](_page_26_Figure_7.jpeg)

Question 4

4.1 Use the graph above to complete the table.

X	-2	-1	с	d	2	3
У	a	b	3	4	e	f

4.2 Determine a function rule to describe the relationship between x and y.

![](_page_26_Picture_12.jpeg)

![](_page_27_Picture_0.jpeg)

![](_page_27_Picture_1.jpeg)

# Question 5

Describe and correct the error in graphing the function represented by the input-output table.

Х	-4	-2	0	2
У	-1	1	3	5

![](_page_27_Figure_5.jpeg)

# Question 6

Match the graph with the function rule it represents.

![](_page_27_Figure_8.jpeg)

The End

![](_page_27_Picture_10.jpeg)

![](_page_28_Picture_0.jpeg)

![](_page_28_Picture_1.jpeg)

### **ASSESSMENT / REVISION TASK**

GRADE: 9

## **TOPIC: FUNCTIONS & RELATIONSHIPS** MEMORANDUM

### Question 1

Madison: A function is a relationship that assigns exactly one output value for each input value.

The input value of five has two outputs. It has an output of two and nine. So that input value of five does not have exactly one output; it has two. That means this figure cannot represent a function. So, our answer is: False.

#### Question 2

### 2.1

а	y = 4x	$\therefore y = 4 \times \frac{1}{2}$	$\therefore y = 2$
---	--------	---------------------------------------	--------------------

- b y = 4x  $\therefore y = 4 \times \frac{1}{4}$   $\therefore y = 1$
- c y = 4x  $\therefore y = 4 \times \frac{-1}{4}$   $\therefore y = -1$   $\therefore y = -1$   $\therefore y = -2$

### 2.2

e
$$y = \frac{x}{2}$$
 $\therefore e \leftarrow multiply by 2 \leftarrow 8$  $\therefore 16 \leftarrow multiply by 2 \leftarrow 8$ f $y = \frac{x}{2}$  $\therefore f \leftarrow multiply by 2 \leftarrow 5$  $\therefore 10 \leftarrow multiply by 2 \leftarrow 5$ g $y = \frac{x}{2}$  $\therefore g \leftarrow multiply by 2 \leftarrow 2$  $\therefore 4 \leftarrow multiply by 2 \leftarrow 2$ h $y = \frac{x}{2}$  $\therefore h \leftarrow multiply by 2 \leftarrow 1$  $\therefore 2 \leftarrow multiply by 2 \leftarrow 1$ 

2.3

2.3.1  $\left\{\frac{1}{2}, \frac{1}{4}, \frac{-1}{4}, \frac{-1}{2}\right\} \rightarrow \text{rational numbers}$ 2.3.2  $\{16; 10; 4; 2\} \rightarrow \text{natural numbers}$ 

![](_page_28_Picture_18.jpeg)

![](_page_29_Picture_0.jpeg)

![](_page_29_Picture_1.jpeg)

## Question 3

3.1

![](_page_29_Figure_4.jpeg)

## 3.2 Output will increase by 3

#### 3.3

Input	6	7	8	9	
$3 \times x$	3 × 6	3 × 7	3 × 8	3× 9	
$3 \times x - 2$	$3 \times 6 - 2$	$3 \times 7 - 2$	$3 \times 8 - 2$	3 × 9 – 2	
Output	16	19	22	25	

$$\therefore y = 3x - 2$$

#### Question 4

4.1

х	-2	-1	0	1	2	3
У	1	2	3	4	5	6

### 4.2

Constant difference: +1

Input	-2	-1	0	1	2	3
$1 \times x$	1 × -2	1 × -1	1 × 0	1 × 1	1 × 2	1 × 3
$1 \times x + 3$	$1 \times -2 + 3$	$1 \times -1 + 3$	$1 \times 0 + 3$	$1 \times 1 + 3$	$1 \times 2 + 3$	$1 \times 3 + 3$
Output	1	2	3	4	5	6

 $\therefore y = x + 3$ 

![](_page_29_Picture_16.jpeg)

![](_page_30_Picture_0.jpeg)

Question 5

![](_page_30_Picture_2.jpeg)

The ordered pairs are written incorrectly from the table and therefor plotted wrong on the Cartesian plane.

The *x* coordinate , which is the input value is always first.

The *y coordinate*, which is the output value is second.

Therefore : (x - coordinate; y - coordinate)

![](_page_30_Figure_7.jpeg)

## Question 6

Choose any coordinate on a straight line and substitute into respective equation.

( <b>0</b> ; <b>1</b> ): $y = x + 1$	(2; 3): $y = x + 1$	
$\therefore y = (0) + 1$	$\therefore y = (2) + 1$	: <b>6.1</b> $y = x + 1$ (B)
$\therefore y = 1$	$\therefore y = 3$	
(1; 4): y = -2x + 6	(3; 0): $y = -2x + 6$	
$\therefore y = -2(1) + 6$	$\therefore y = -2(3) + 6$	$\therefore$ <b>6</b> . <b>2</b> $y = -2x + 6$ ( <i>C</i> )
$\therefore y = -2 + 6$	$\therefore y = -6 + 6$	
$\therefore y = 4$	$\therefore y = 0$	
<b>(0; 0)</b> : $y = \frac{x}{3}$	(3; 1): $y = \frac{x}{3}$	
$\therefore y = \frac{0}{3}$	$\therefore y = \frac{3}{3}$	$\therefore 6.3 \ y = \frac{x}{3}  (A)$
$\therefore y = 0$	$\therefore y = 1$	

The End

![](_page_30_Picture_12.jpeg)

**Functions and Relationships**